

Automatic optimization and multi-scale delineation of nested slope units with r.slopeunits v2.0

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ISTITUTO DI RICERCA PER LA PROTEZIONE IDROGEOLOGICA

CONSIGLIO NAZIONALE DELLE RICERCHE

(PERUGIA, ITALY)



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A story about complaining

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DIFFERENT MAPPING UNITS

Possible choices for mapping units in landslide studies:

- **Grid Cells:** typically aligned with a digital elevation model (DEM) grid. Have little relation with the underlying topographic properties but are by far the **standard choice**.
- **Terrain units (TU):** subdivisions of the terrain that **maximize** the within-unit (internal) **homogeneity** and the between-unit (external) inhomogeneity across distinct physical or geographical boundaries.
- **Slope unit (SU):** morphological TU **bounded by drainage and divide lines**. Slope Units are a wiser mapping unit choice for a variety of applications, for they bear a strong relationship with topography.

Carrara et al. (1991); Guzzetti et al. (1999)

SLOPE UNITS: MOTIVATION

- SU are real-world features, easily recognizable **in the field**
- Related to hydrological and geo-morphological processes that shape natural landscapes
- Minimize mapping errors: use data sources of **different type** and **resolution**



- Well suited for hydro- and geo-morphological studies
- Typical example: **landslide susceptibility zonation**
- Also useful to reconcile models with different models and zonation

SLOPE UNITS

MOTIVATION

- You are real world
- First round of complaining!
- Related to hydrological and geo-morphological processes that shape natural
- “...I do not know how to draw slope units!”
- Minimize mapping errors: use data sources of different type and resolution
- “...it is too tedious to do it manually...”
- “...my slope units are different from those delineated by my colleague!”
- Typical examples
- Also useful to reconcile models with different models and zonation (part 4)

THE `r.slopeunits` GRASS GIS MODULE

(Main) Inputs:

- **DEM**
- Initial flow **accumulation THRESHOLD**
- Aspect **homogeneity** (circular variance, **C**)
- Tentative SU **minimum area (A)**

Output:

SLOPE UNITS POLYGONAL MAP

Alvioli et al., GMD (2016)

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ADAPTIVE SLOPE UNITS DELINEATION

The software `r.slopeunits` implements an **iterative** algorithm:

- An **initial subdivision** is calculated by `r.watershed` with a **trial (large) flow accumulation threshold**
- At **each iteration**, half-basins are **checked against** input parameters constraints (*c*, homogeneity; *a*, size)
- Only those *half-basins not meeting the requirements*, are **split further** at next iteration by `r.watershed` with a **smaller accumulation threshold**



ADAPTIVE *SU* DELINEATION

Alvioli et al., GMD (2016)

M. Alvioli



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PARAMETRIC SLOPE UNITS DELINEATION

- The **r.watershed** model defines **half-basins of decreasing size** at each iteration

For a given value of

flow accumulation

threshold t :

STREAM



PARAMETRIC SLOPE UNITS DELINEATION

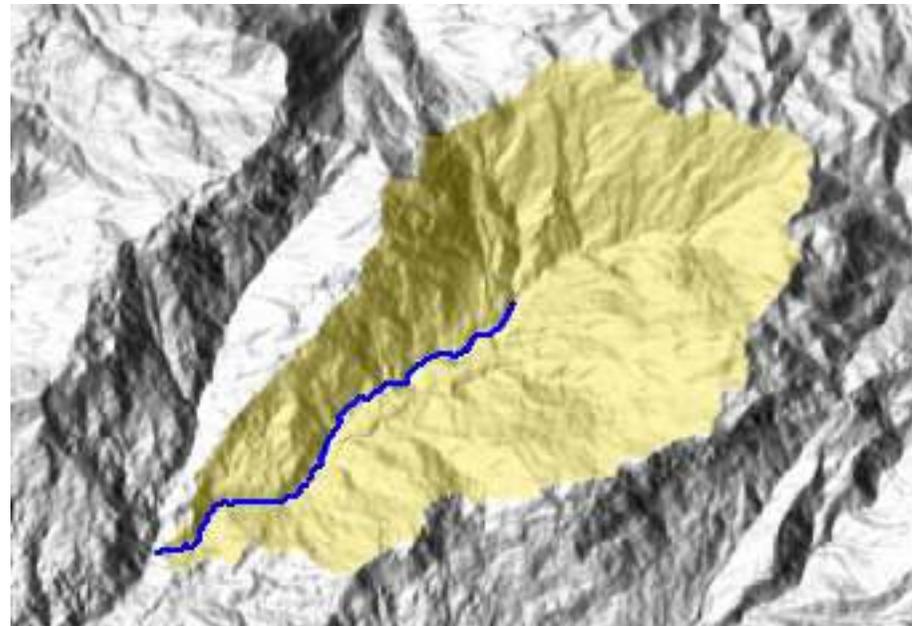
- The **r.watershed** model defines **half-basins of decreasing size** at each iteration

For a given value of

flow accumulation

threshold t :

Drainage BASIN



PARAMETRIC SLOPE UNITS DELINEATION

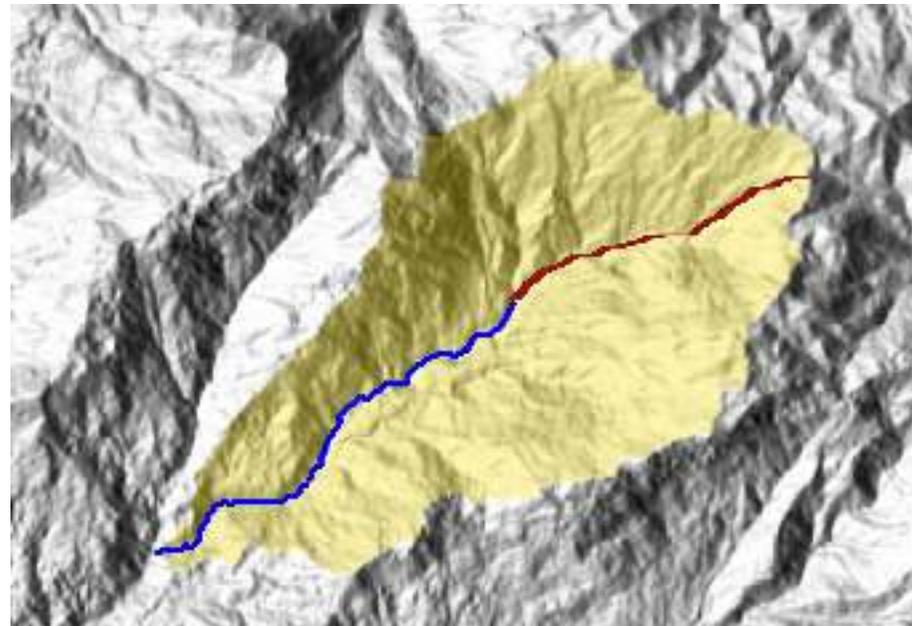
- The **r.watershed** model defines **half-basins of decreasing size** at each iteration

For a given value of

flow accumulation

threshold t :

EXTENDED STREAM



PARAMETRIC SLOPE UNITS DELINEATION

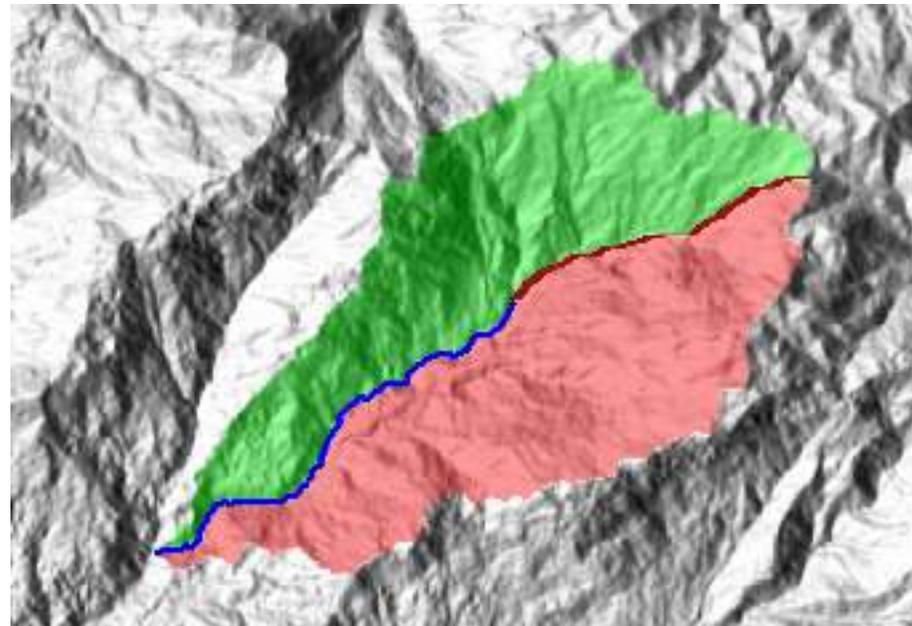
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For a given value of

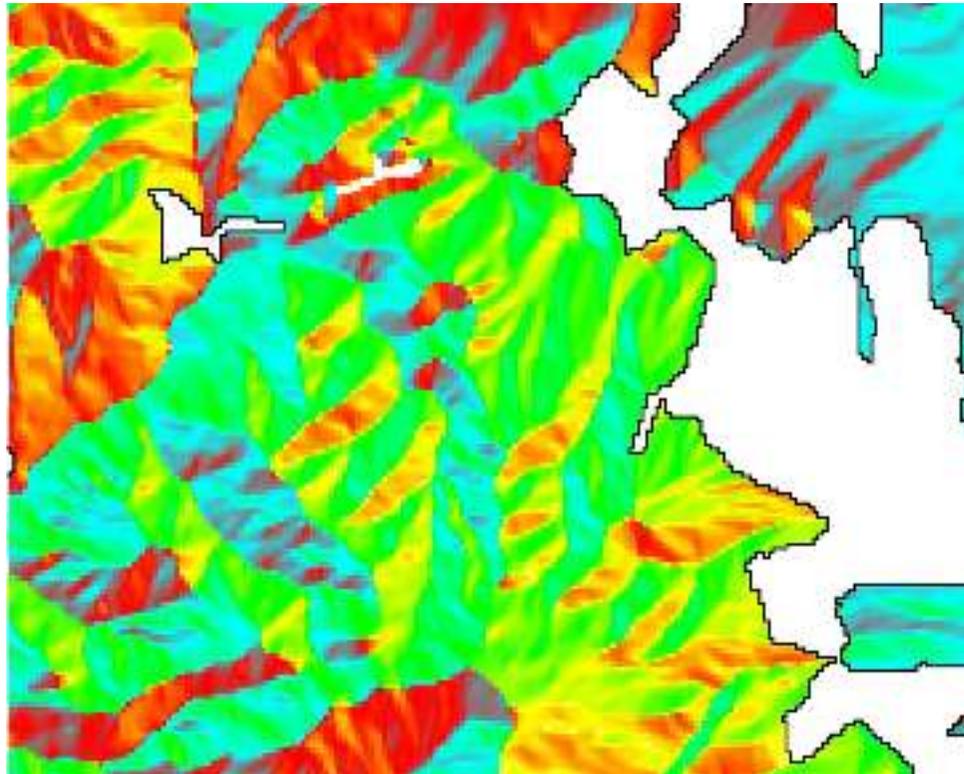
flow accumulation

threshold t :

LEFT - RIGHT
HALF BASINS



PARAMETRIC SLOPE UNITS DELINEATION

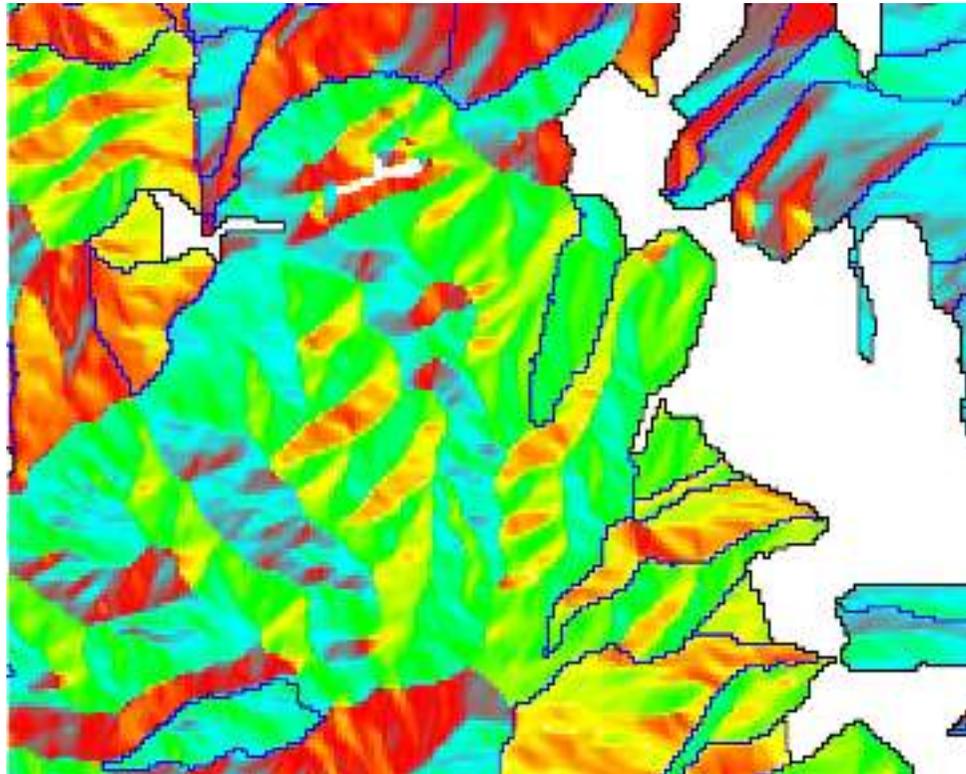


Example of r.slopeunits run

- Plains are in white
- Different aspect directions are in red, green, yellow, cyan

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



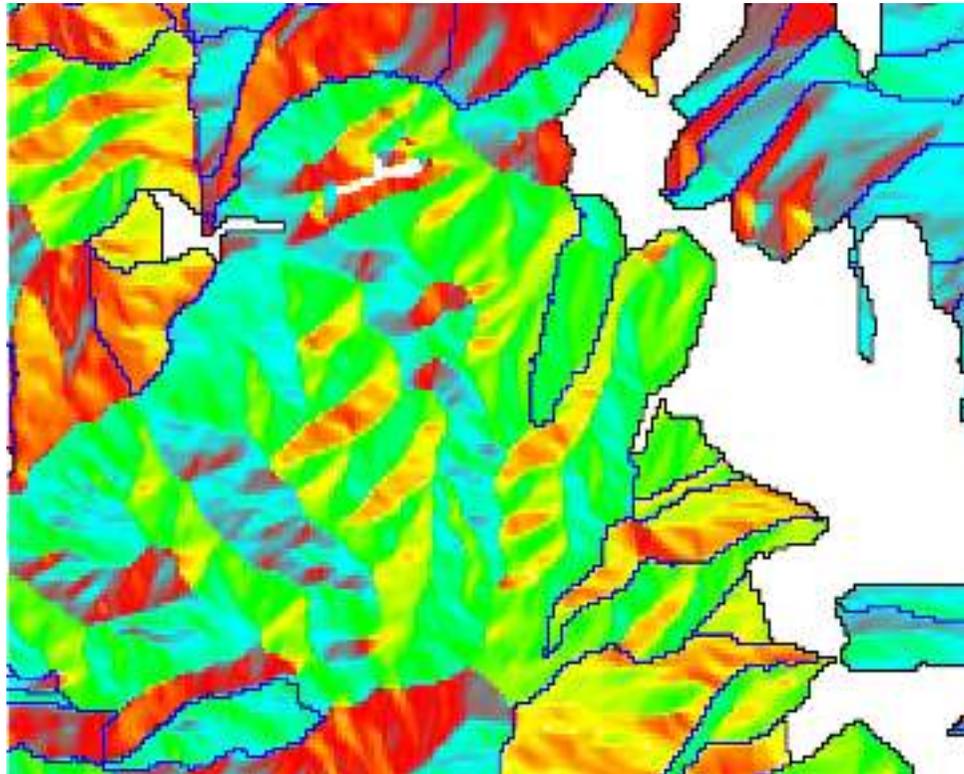
Example of r.slopeunits run

Iteration #1:

HB_{child} flagged as slope units
are in blue

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



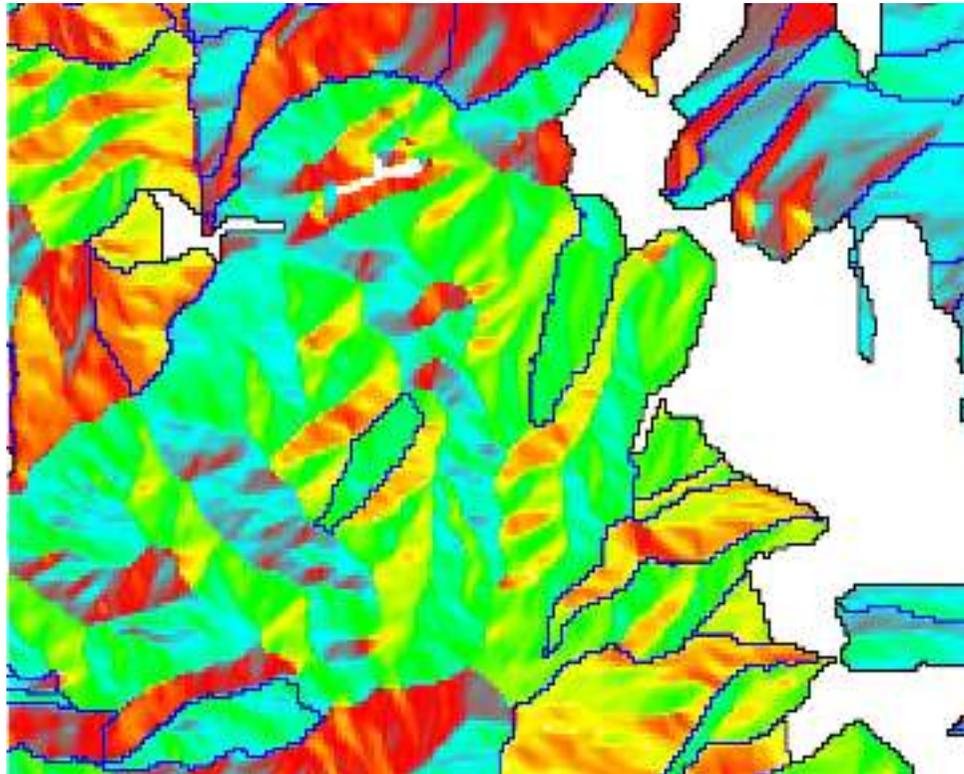
Example of r.slopeunits run

Iteration #5:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



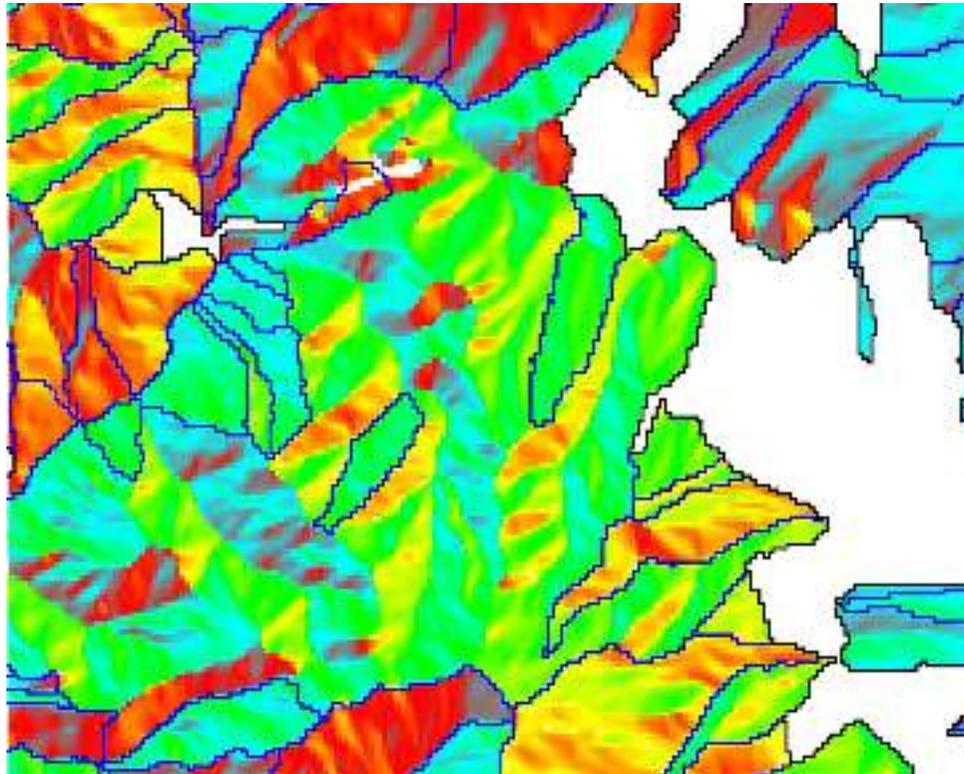
Example of r.slopeunits run

Iteration #10:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



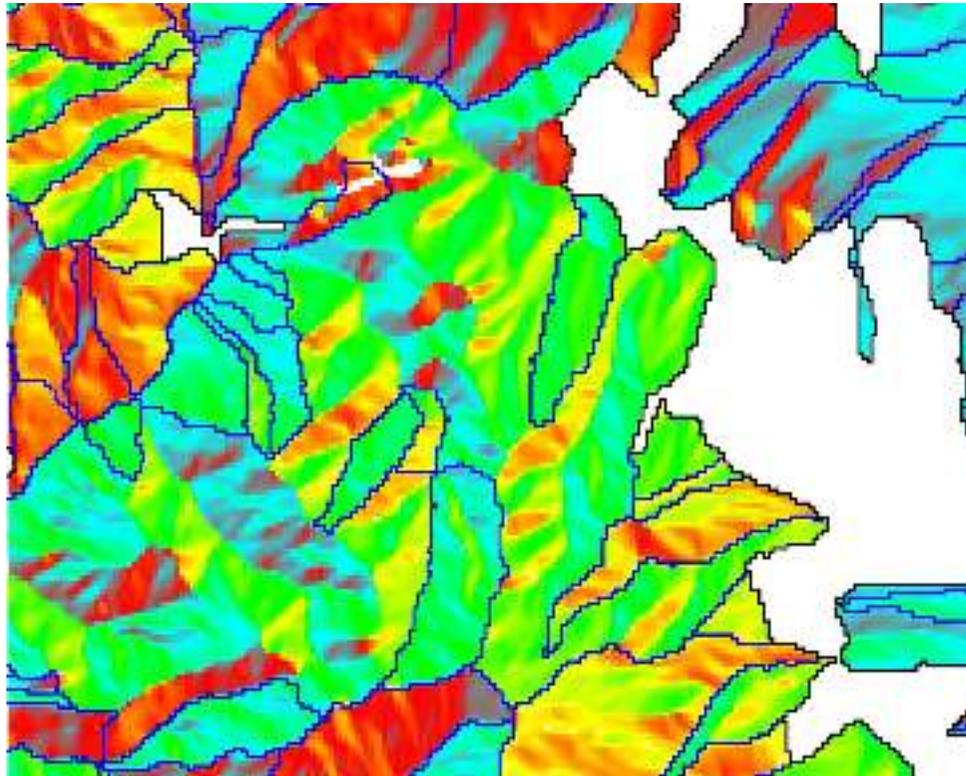
Example of r.slopeunits run

Iteration #15:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



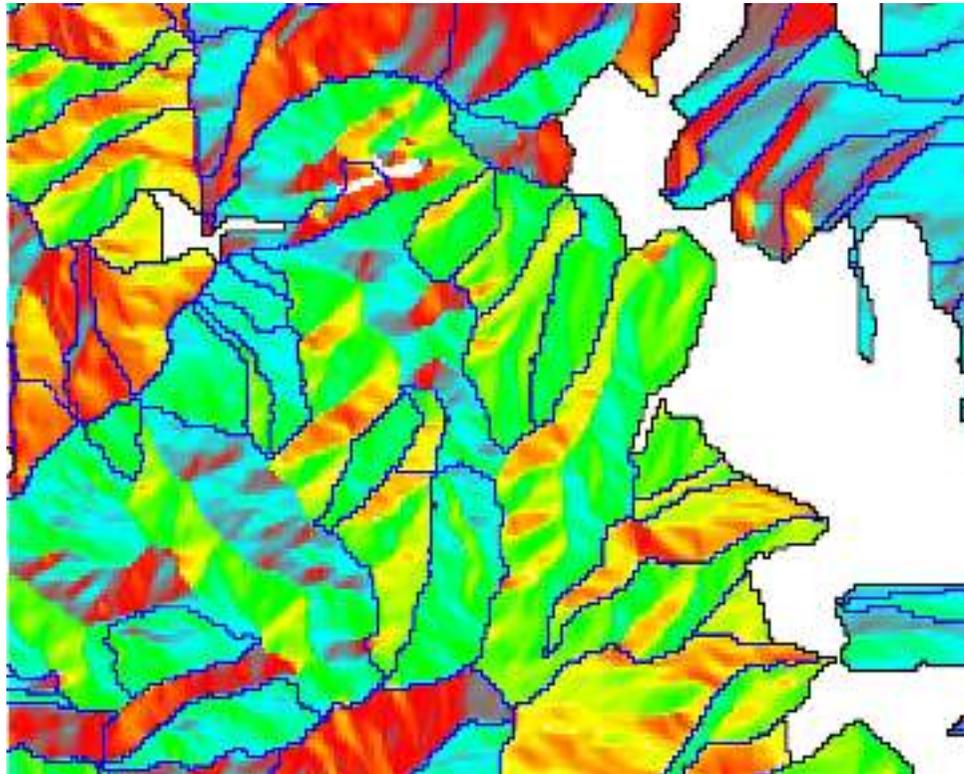
Example of r.slopeunits run

Iteration #20:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



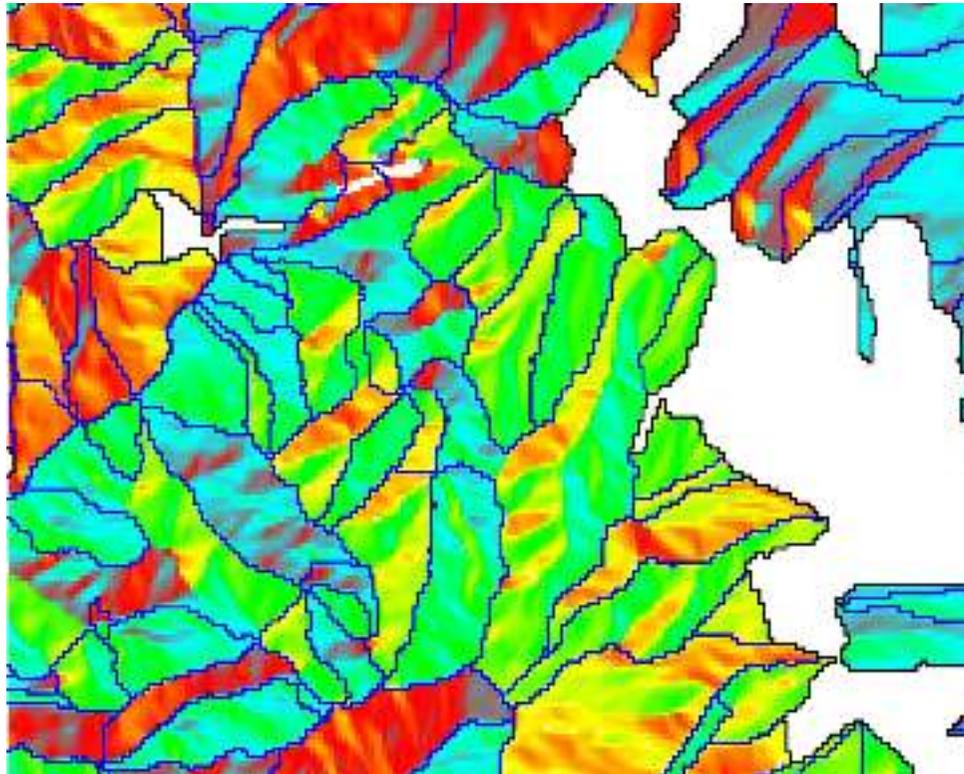
Example of r.slopeunits run

Iteration #25:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



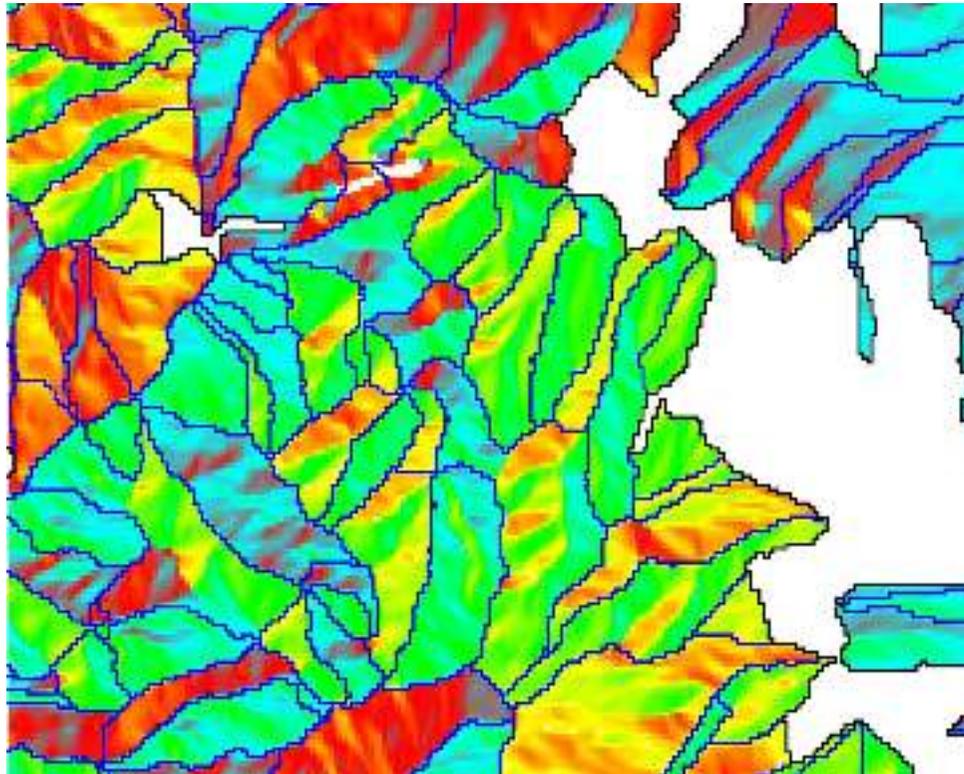
Example of r.slopeunits run

Iteration #30:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



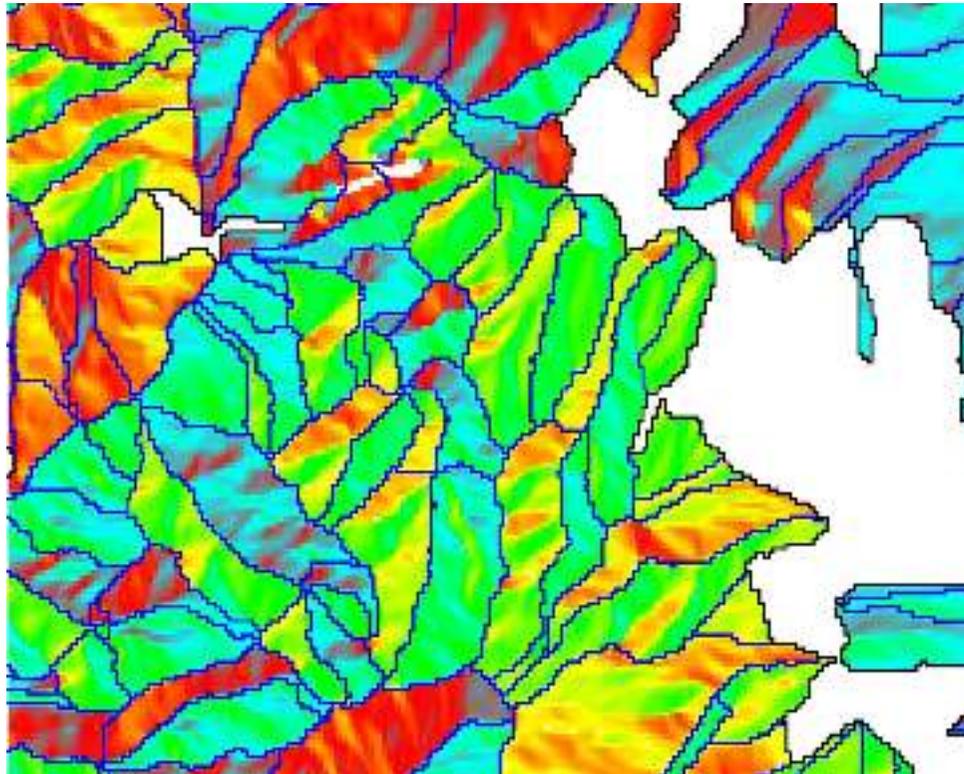
Example of r.slopeunits run

Iteration #35:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



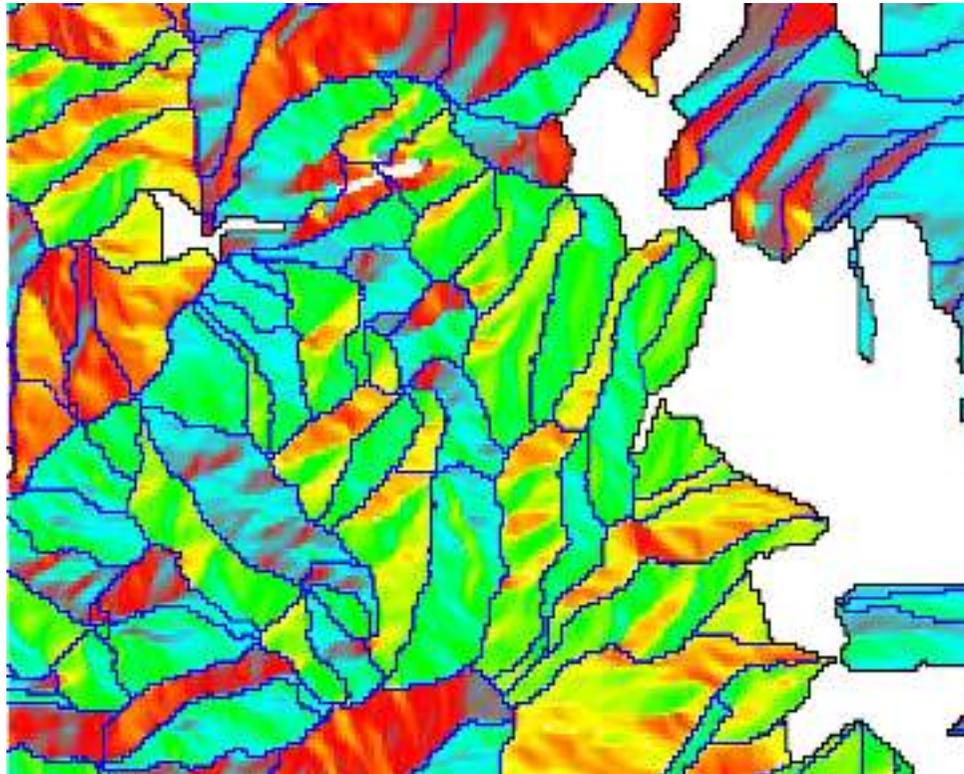
Example of r.slopeunits run

Iteration #40:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



Example of r.slopeunits run

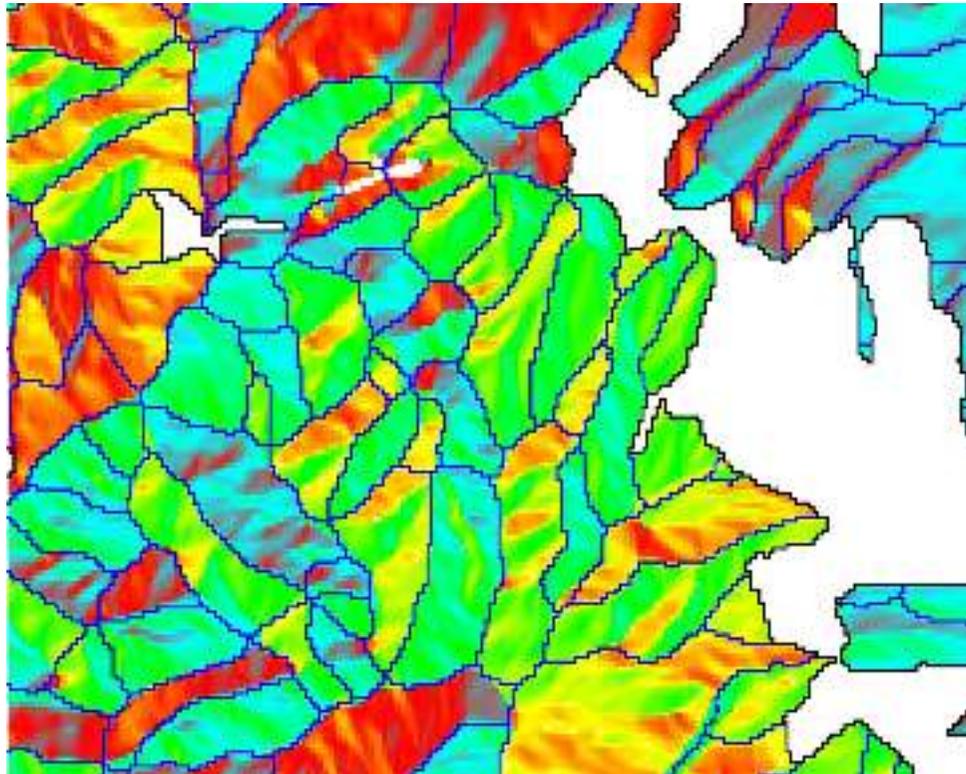
Iteration #45:

A few polygons (in blue) were added to the candidate slope unit set – not all of the values of t produces new candidates

No new half-basins could be added after this step

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION

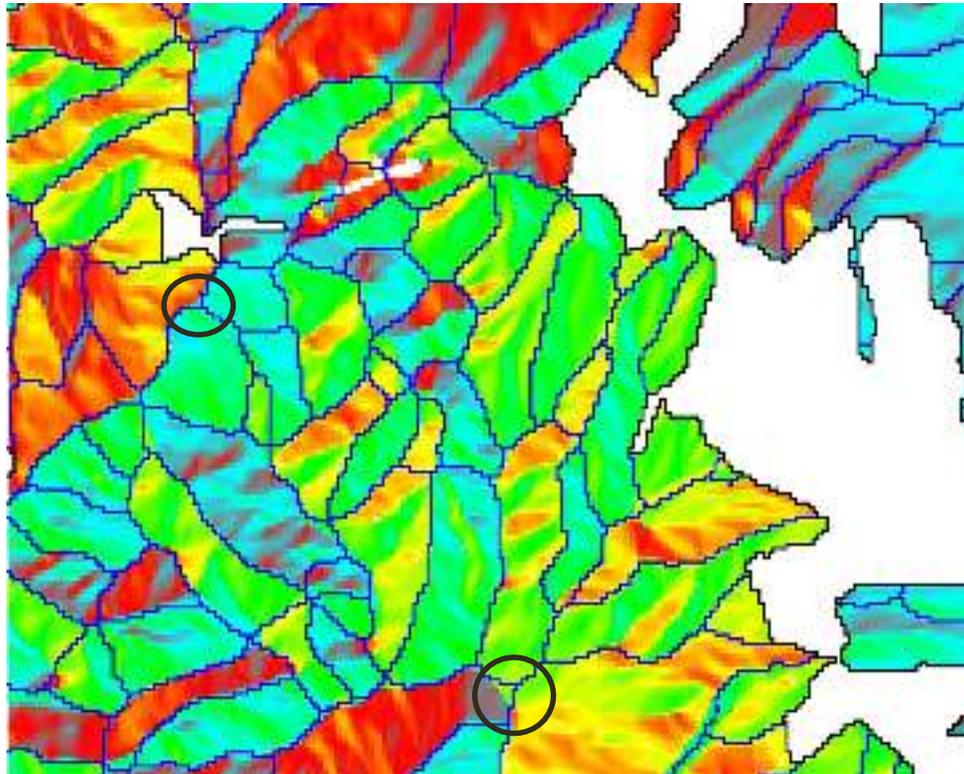


Example of r.slopeunits run

Cleaning of the final SU map using the procedure n. 2: removal of small (smaller than *cleansize*), elongated and narrow polygons

Alvioli et al., GMD (2016)

PARAMETRIC SLOPE UNITS DELINEATION



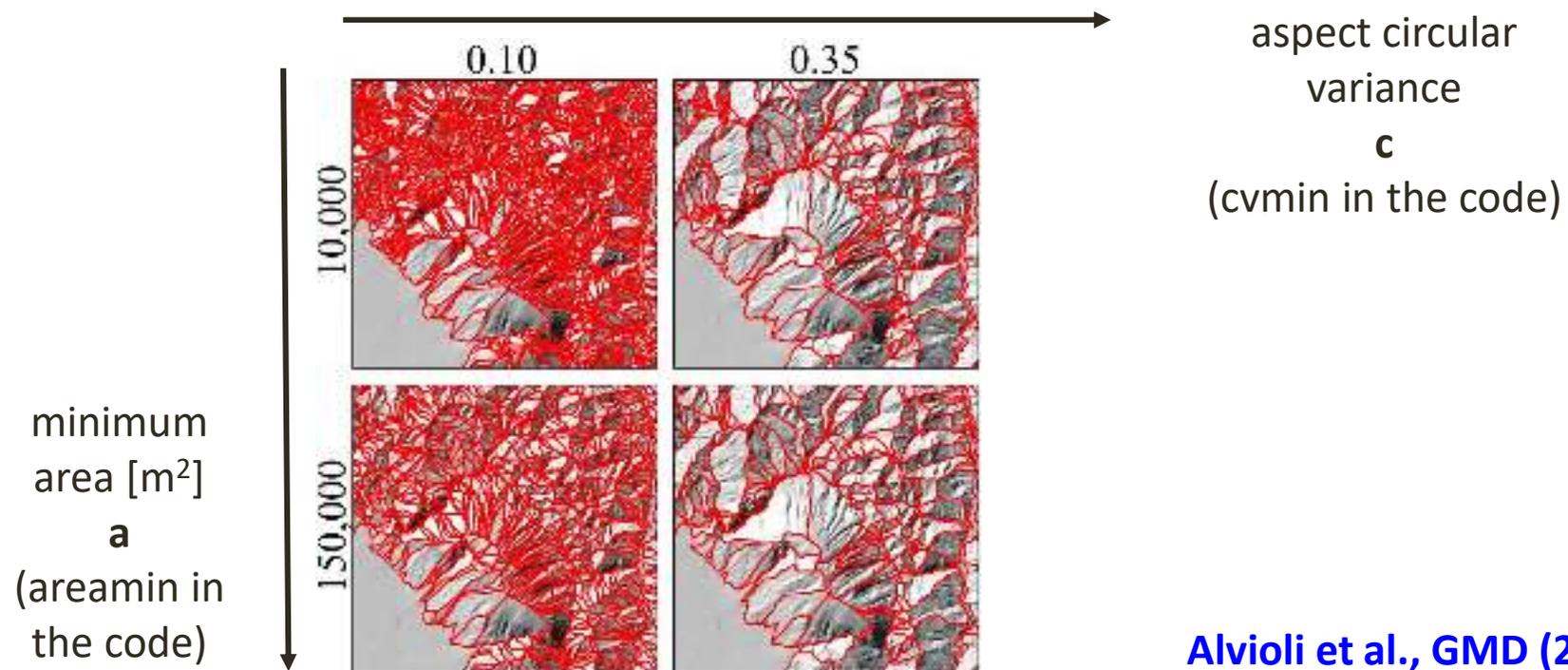
Example of r.slopeunits run

Cleaning of the final SU map using the procedure n. 2: removal of small (smaller than *cleansize*), elongated and narrow polygons

Note that small errors may be introduced by this procedure as well – this may be viewed as a trial-and-error step

PARAMETRIC SLOPE UNITS DELINEATION

Each combination of the a , c parameters determines a **well-defined SU subdivision**



Alvioli et al., GMD (2016)

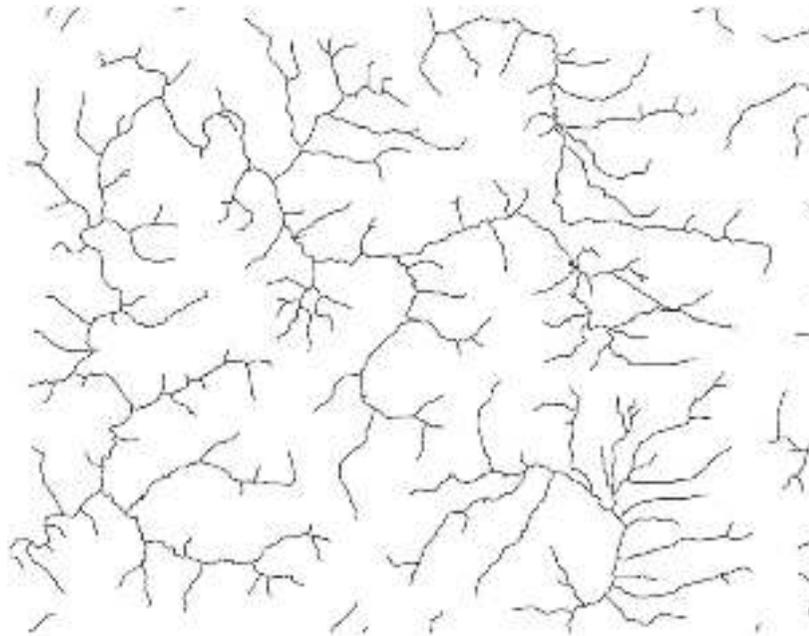
CHALLENGES IN SLOPE UNITS DELINEATION

Need to stop the process at the *right scale*

Drainage Network



Half-Basins



WATERSHED THRESHOLD: 5000 CELLS



WATERSHED THRESHOLD: 5000 CELLS

Second round of complaining!

“...I don't know how to select input parameters!”

“...I do not want to run the code several times with different parameters!”

WATERSHED THRESHOLD: 5000 CELLS

WATERSHED THRESHOLD: 5000 CELLS

SLOPE UNITS OPTIMIZATION: ASPECT SEGMENTATION METRIC

Aspect segmentation metric $F(\mathbf{a}, \mathbf{c})$: measures internal homogeneity/external inhomogeneity

$$V = V(\mathbf{a}, \mathbf{c}) = \frac{\sum_n^N c_n S_n}{\sum_n^N c_n}$$

$$I = I(\mathbf{a}, \mathbf{c}) = \frac{N \sum_{n,l}^N \omega_{n,l} (\alpha_n - \bar{\alpha})(\alpha_l - \bar{\alpha})}{\sum_n^N (\alpha_n - \bar{\alpha})^2 \sum_{n,l}^N \omega_{n,l}}$$

$$F = F(\mathbf{a}, \mathbf{c}) = \frac{V_{max} - V(\mathbf{a}, \mathbf{c})}{V_{max} - V_{min}} + \frac{I_{max} - I(\mathbf{a}, \mathbf{c})}{I_{max} - I_{min}}$$

- $V(\mathbf{a}, \mathbf{c})$ represents **internal aspect variance** and assigns more importance to large SUs to avoid numerical instabilities
- $I(\mathbf{a}, \mathbf{c})$ is an autocorrelation index, measures **external aspect variance** and has minima for SU sets exhibiting well-defined boundaries between adjacent SUs

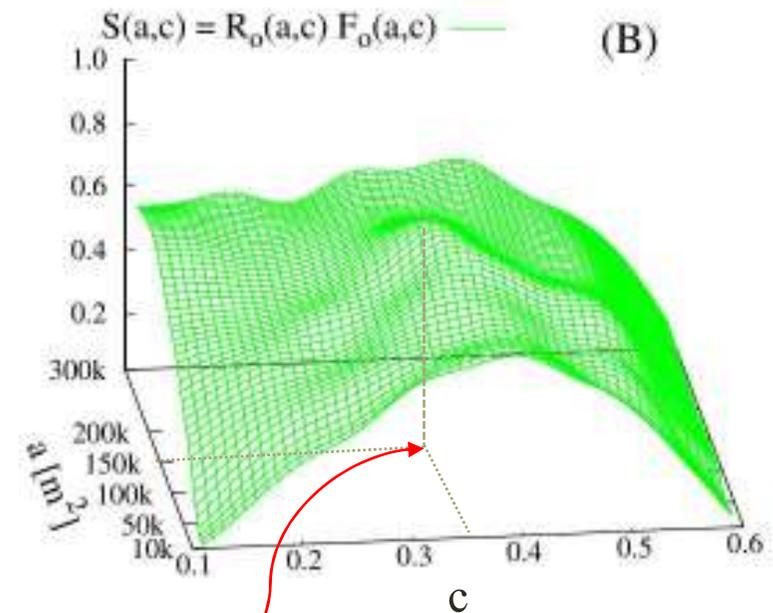
Espindola et al., Int. J. Rem. Sens. (2016)

SLOPE UNITS DELINEATION & OPTIMIZATION

No unique SU subdivision exists!

We follow a workflow:

- Parametric delineation
- Calculation of the metric(s)
- Optimization (**r.slopeunits v2.0**)
- Landslide susceptibility modeling with statistical and/or machine learning model

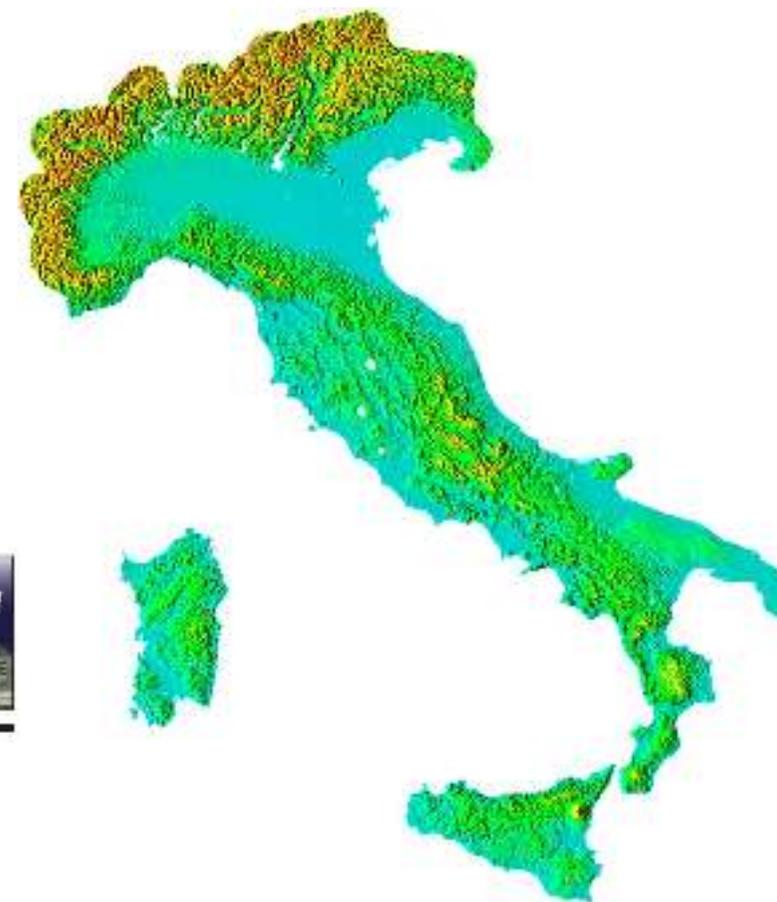


optimal
values

Alvioli et al., GMD (2016)
Alvioli et al., (this conference)

EXAMPLE: SLOPE UNITS OF ITALY

- Number of polygons: 331,926
- Average area: 0.45 km²
- Total coverage: 224,000 km²
(excludes near-flat areas)



Alvioli et al., Geomorphology (2020)

GRASS GIS R.SLOPEUNITS TOOLSET

r.slopeunits - Toolset for calculating metrics for slope units

DESCRIPTION

- *r.slopeunits* is a GRASS GIS addon toolset that creates, cleans and calculate metrics for slope units. Additionally, optimal input values can be determined. The *r.slopeunits* toolset consists of currently four modules:
- [r.slopeunits.create](#): Creates a raster layer of slope units. Optionally, a vector map.
- [r.slopeunits.clean](#): Cleans slope units layer, e.g. results of *r.slopeunits.create*.
- [r.slopeunits.metrics](#): Creates metrics for slope units.
- [r.slopeunits.optimize](#): Determines optimal input values for slope units.

Main authors: Ivan Marchesini, Massimiliano Alvioli, CNR-IRPI
M. Metz, C. Tawalika (translation to Python, refactoring), [mundialis GmbH](#)

GRASS GIS R-SLOPEUNITS TOOLSET

`r.slopeunits`

Third round of complaining!

DESCRIPTION

- `r.slopeunits` is a GRASS GIS add-on toolset that creates, cleans and calculate metrics for slope units of currently used modules.

“...Your optimized slope units are too SMALL!” of

- `r.slopeunits` creates slope units from a DEM.

“...Your optimized slope units are too LARGE!”

- `r.slopeunits` cleans slope units layer, e.g. results of `r.slopeunits:create`.

“...I want several layers of slope units with different size!!”

- `r.slopeunits` determines the optimal slope unit size.

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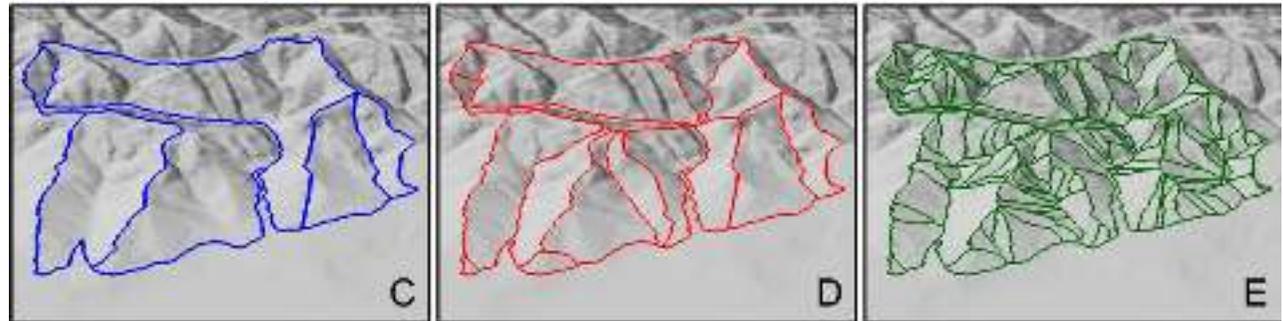
M. Metz, C. Tawanka (translation to Python, refactoring), [mundialis GmbH](#)

PARAMETRIC DELINEATION -> NESTED SLOPE UNITS

- Each combination of the parameters determines a **well-defined SU subdivision**
Alvioli et al., GMD (2016)

- The larger **a** input parameter, the bigger the slope units
- The larger **c** input parameter, the bigger the slope units

- Increasing only one of the two parameters, we get (almost) **nested slope units**



- Adjustment of the edges is necessary



r.slopeunits v2.0

Alvioli et al., (this conference)

NESTED SLOPE UNITS OF ITALY

- We delineated a set of five multi-layer slope unit maps
- Layer 0 is the *existing optimized* SU map
- Layer 0 nested into layer 1
- Layer 1 nested into layer 2
- Layer 2 nested into layer 3
- Layer 3 nested into layer 4
- Layer 4 nested into layer 5
- Nested delineation feature to be published in r.slopeunits v2.1

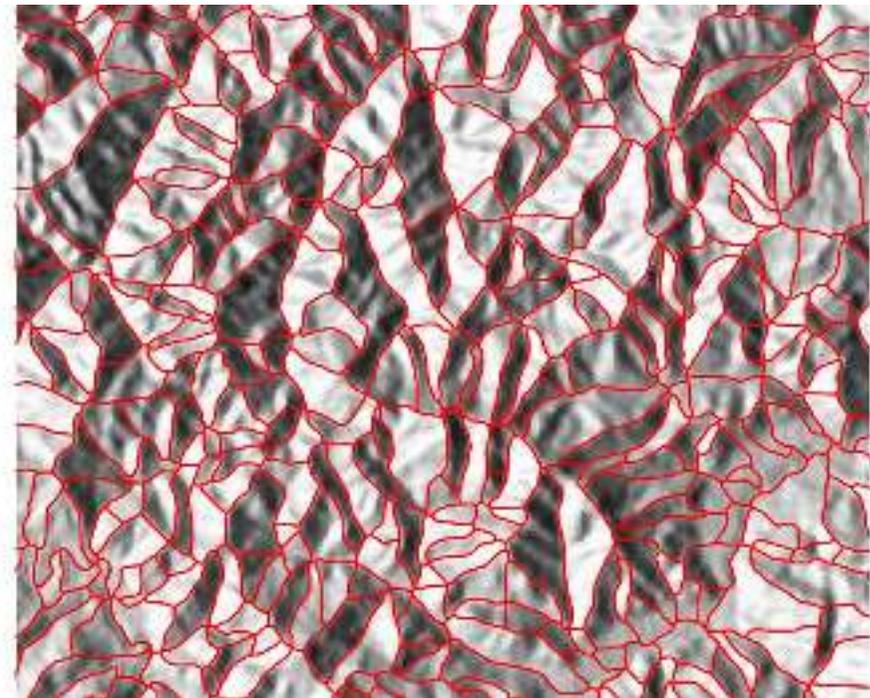
r.slopeunits v2.0



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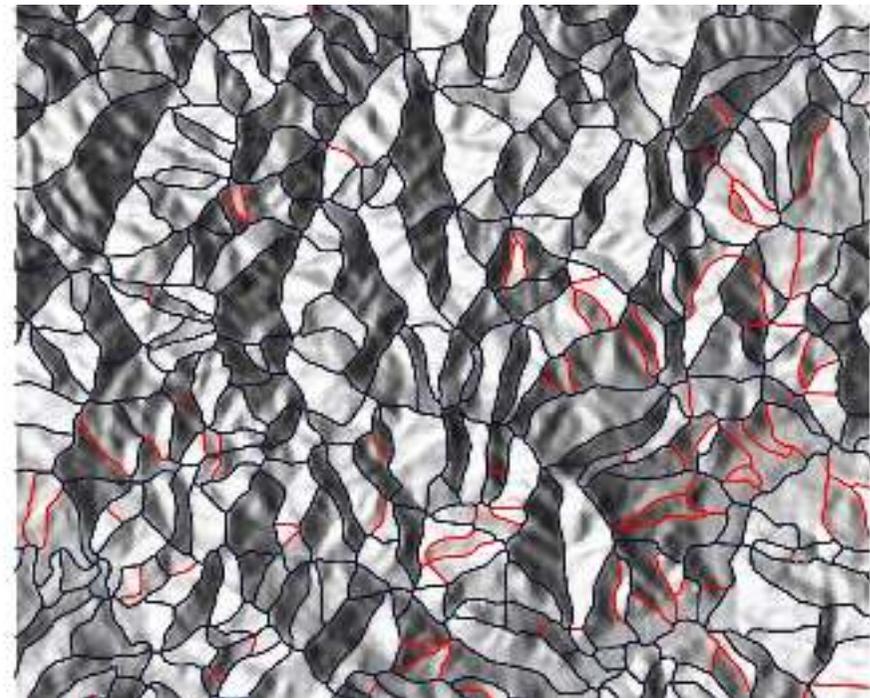
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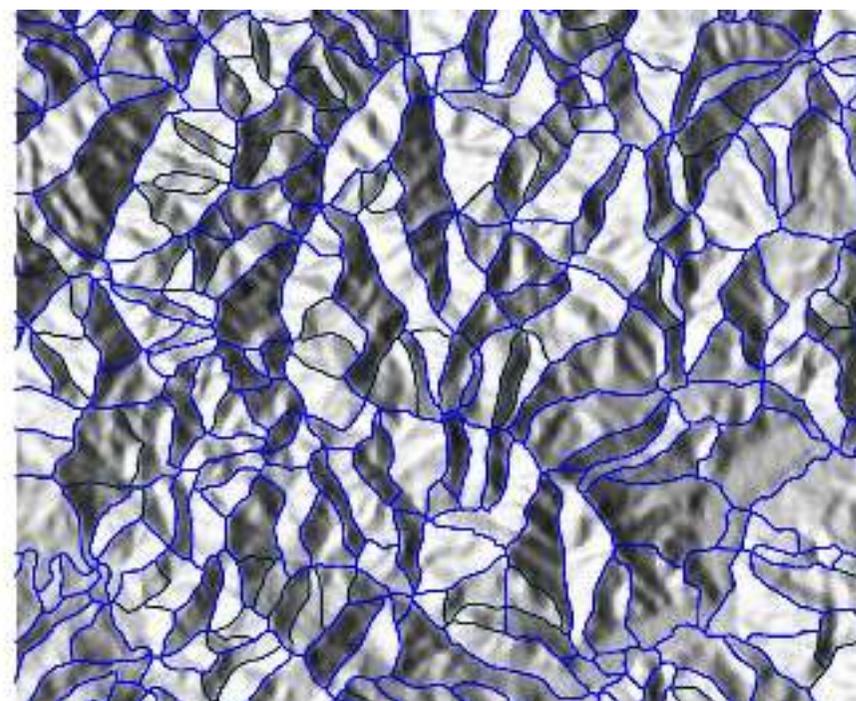
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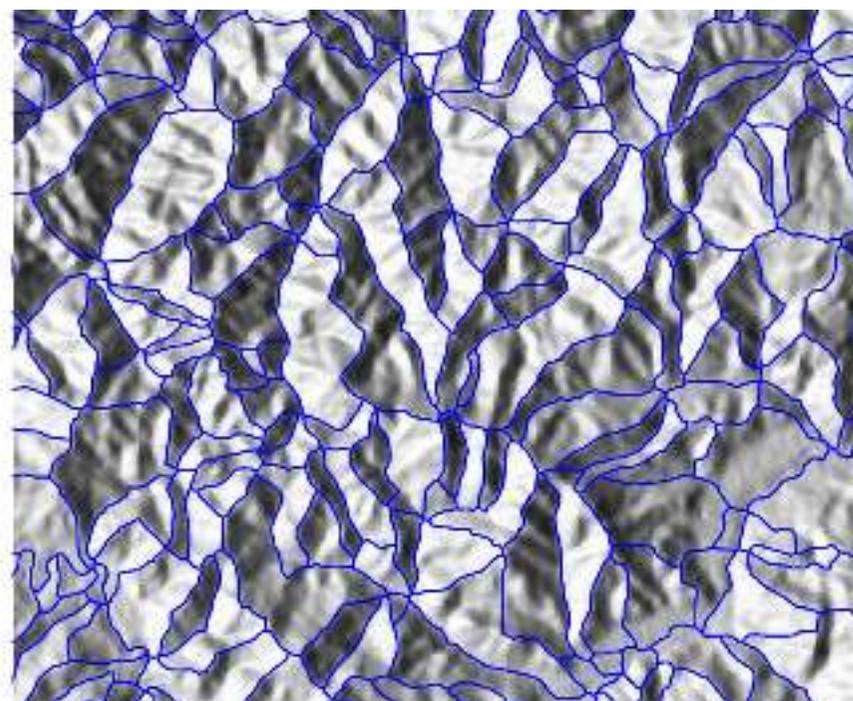
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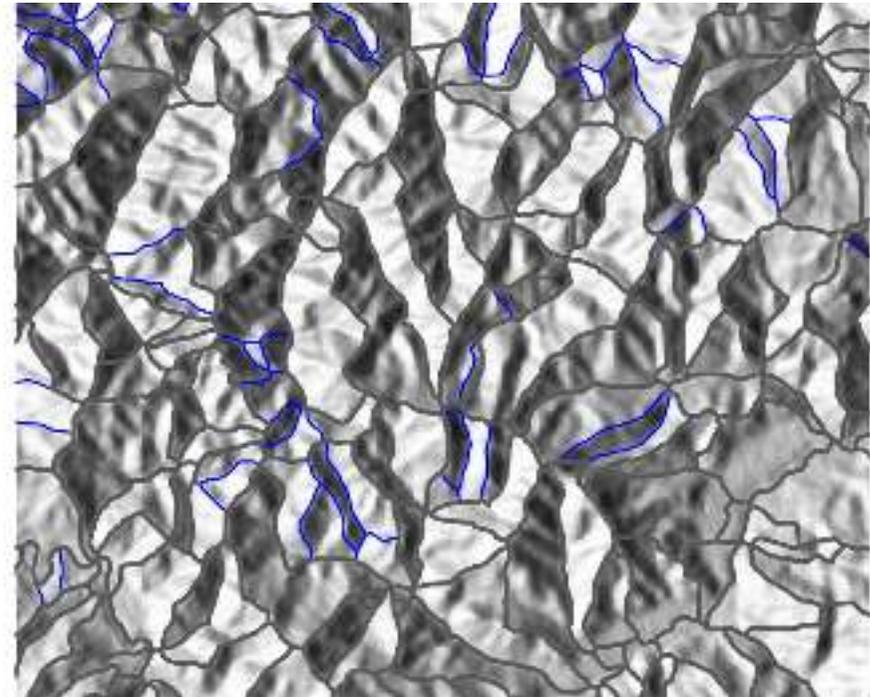
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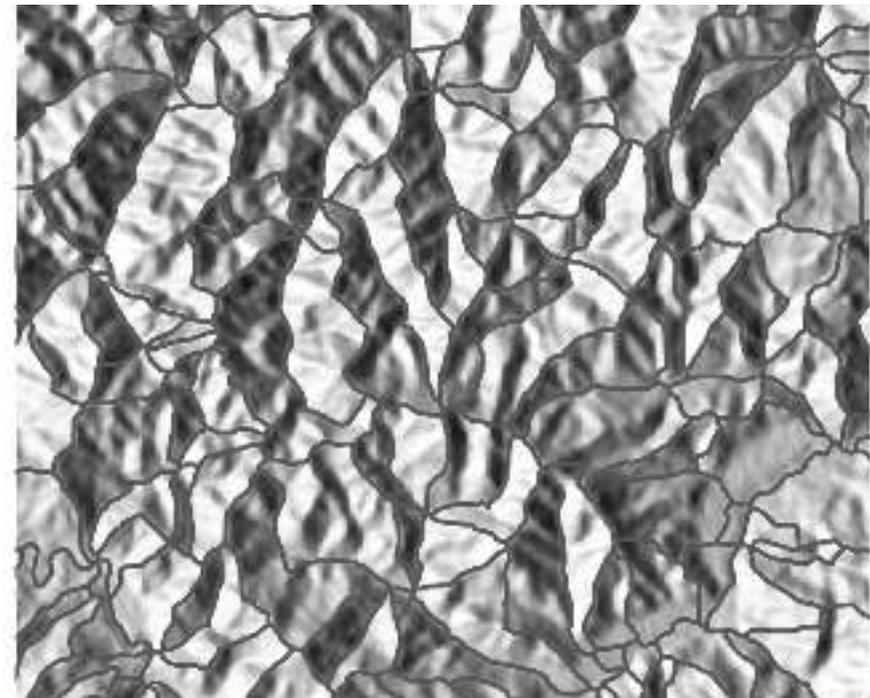
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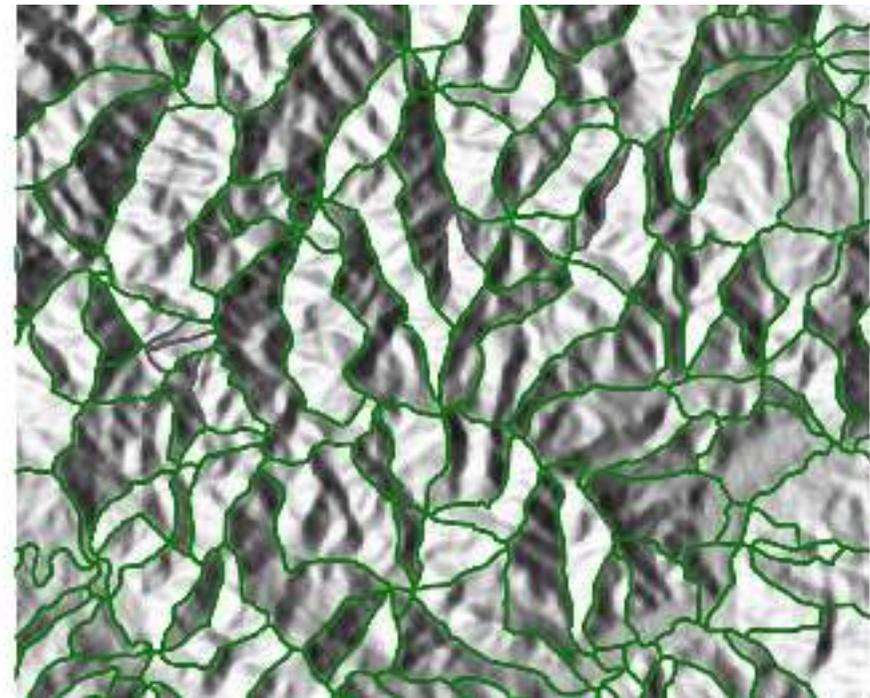
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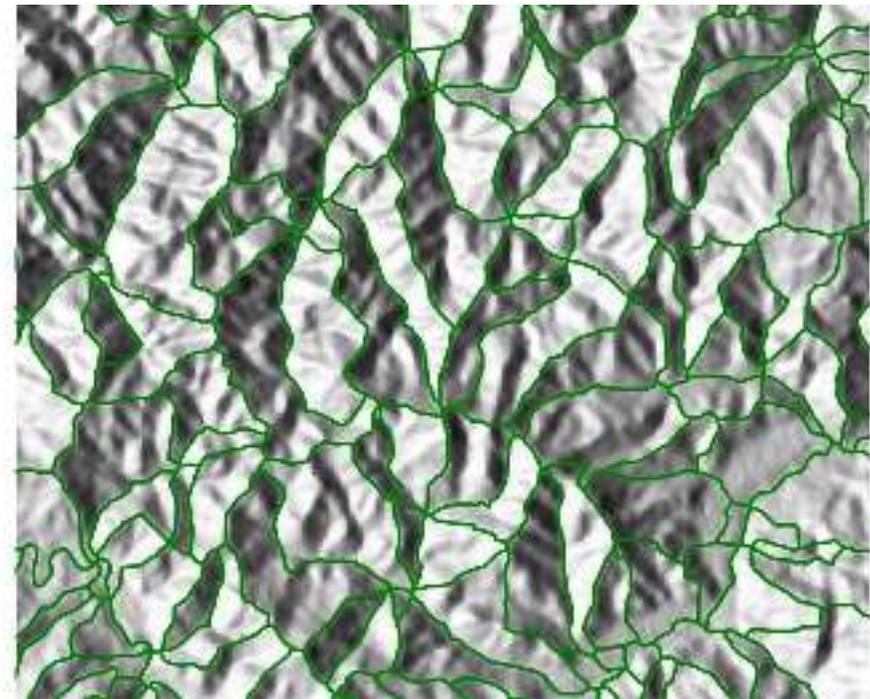
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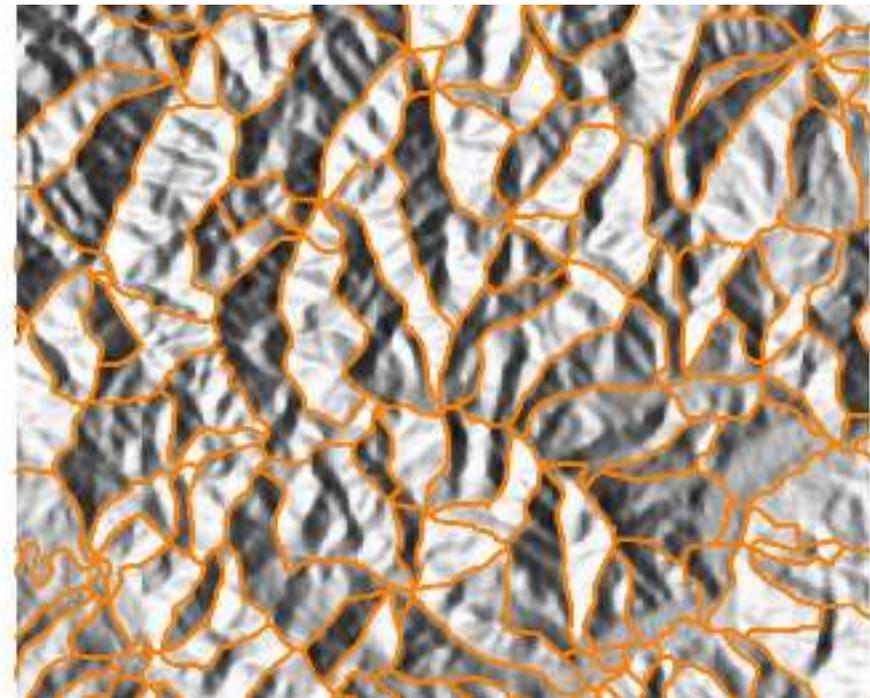
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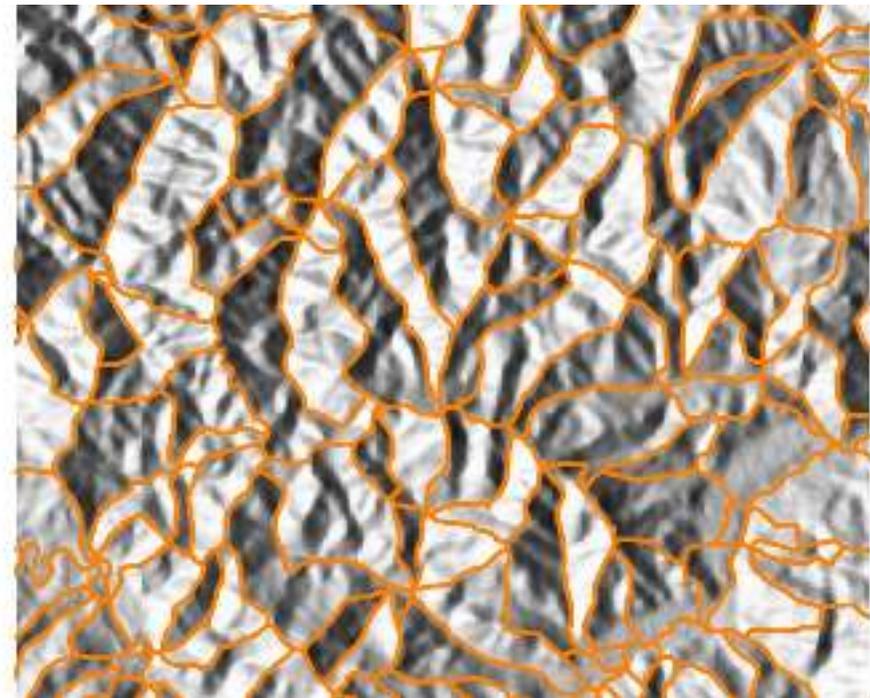
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r.slopeunits v2.0



NESTED SLOPE UNITS OF ITALY

- We prepared a set of five+1 multi-layer slope unit maps

| Layer no. | Minimum area [km ²] | Average area [km ²] | Maximum area [km ²] | Number of polygons | % units with area > average |
|-----------|------------------------------------|------------------------------------|------------------------------------|-----------------------|--------------------------------|
| 0 | 0.092 | 0.69 | 15.51 | 325,578 | 29.9 |
| 1 | 0.096 | 1.02 | 147.73 | 220,308 | 31.2 |
| 2 | 0.096 | 1.32 | 267.46 | 170,240 | 34.3 |
| 3 | 0.096 | 1.55 | 277.20 | 144,430 | 36.5 |
| 4 | 0.096 | 1.67 | 277.20 | 133,928 | 37.1 |
| 5 | 0.096 | 1.72 | 287.81 | 129,961 | 37.3 |

Maps and software available at: <https://geomorphology.irpi.cnr.it/tools/slope-units>

GRASS GIS addon: <https://grass.osgeo.org/grass-stable/manuals/addons/r.slopeunits.html>

CONCLUSIONS: R.SLOPEUNITS IN GRASS GIS

| Feature | v1.0 | v2.0 | v2.1 |
|---------------------------|------|------|------|
| Parametric delineation | ✓ | ✓ | ✓ |
| Adaptive iterative method | ✓ | ✓ | ✓ |
| Parameter optimization | ✗ | ✓ | ✓ |
| Automated installation | ✗ | ✓ | ✓ |
| Nested layers | ✗ | ✗ | ✓ |
| Exclusion of plains | ✗ | ✗ | ✓ |
| Built-in parallelization | ✗ | ✗ | ✓ |

Please keep complaining 😊 and help us improve our software!



Essential BIBLIOGRAPHY

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ADDITIONAL SLIDES



European
Union



Ministero
dell'Agricoltura,
Alimentazione e
Foreste



Il Parlamento
dell'Italia



M. Alvioli



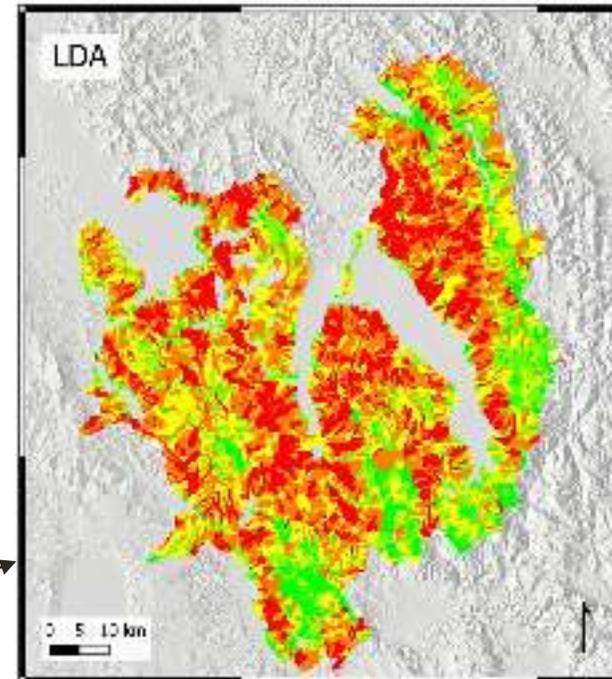
(51)

P2. LANDSLIDE SUSCEPTIBILITY: WHICH METHOD?

Several different methods exist. Results also depend on application strategy:

- Mapping units
- Variable selection
- Data preprocessing, correlations removal
- Training-test strategy, cross validation
- Choice of performance metrics

Same data, same strategy,
different method,
different research group:



Alvioli et al., Earth-Sci. Rev. (2024)

P2. LANDSLIDE SUSCEPTIBILITY: WHICH METHOD?

- We recently compiled a comparative review of landslide susceptibility methods
- 11 independent research groups
- A common dataset
- A common strategy
- All methods explored in detail
- **Benchmark dataset/results:**



<https://geomorphology.irpi.cnr.it/tools/slope-units>

Alvioli et al., Earth-Sci. Rev. (2024)

P2. LANDSLIDE SUSCEPTIBILITY: THE CASE OF ITALY

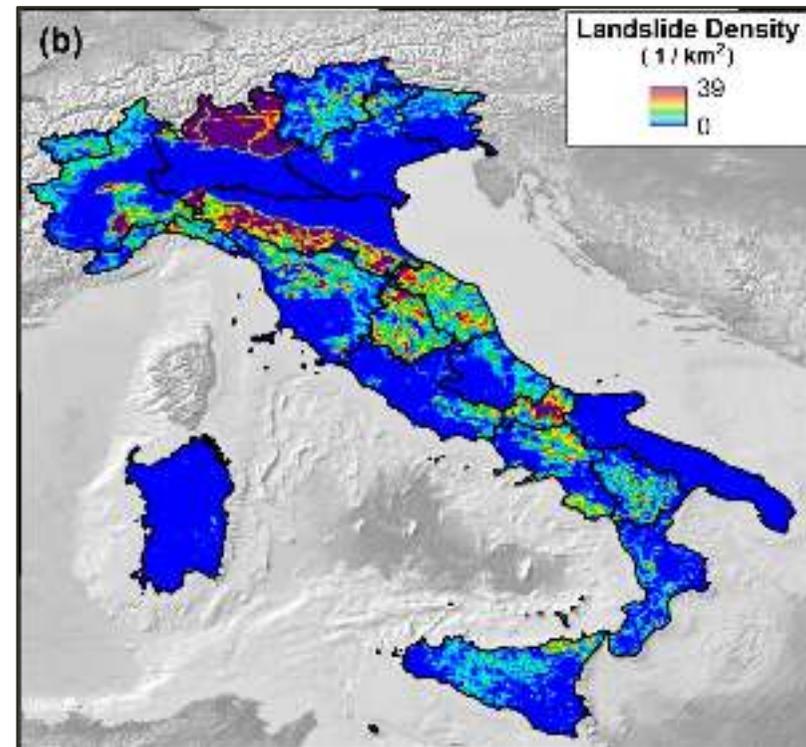
A national landslide inventory exists for Italy:

Inventory compiled independently

- by different people,
- in different regions,
- at different times:

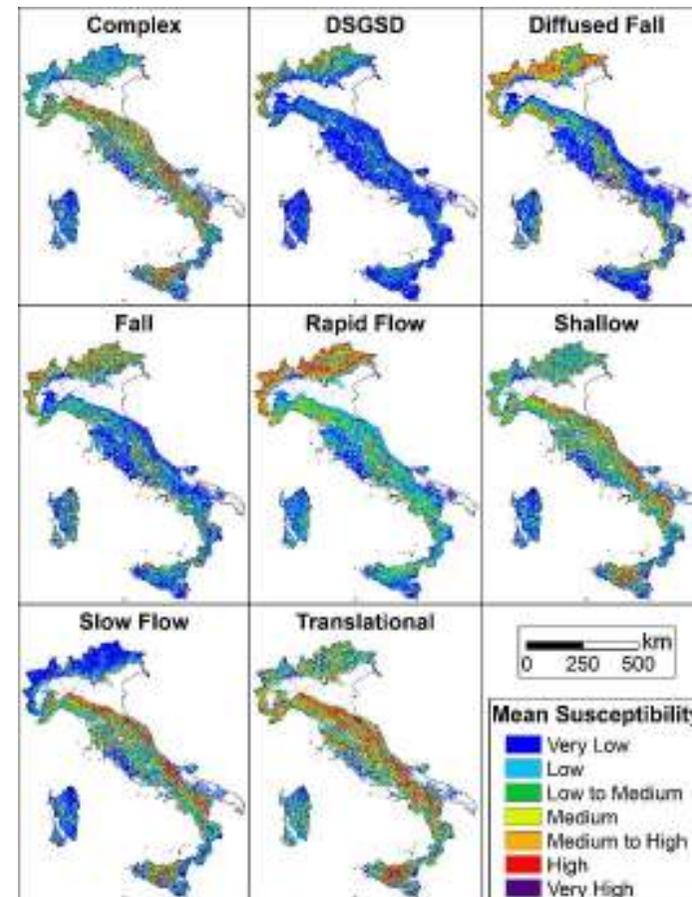
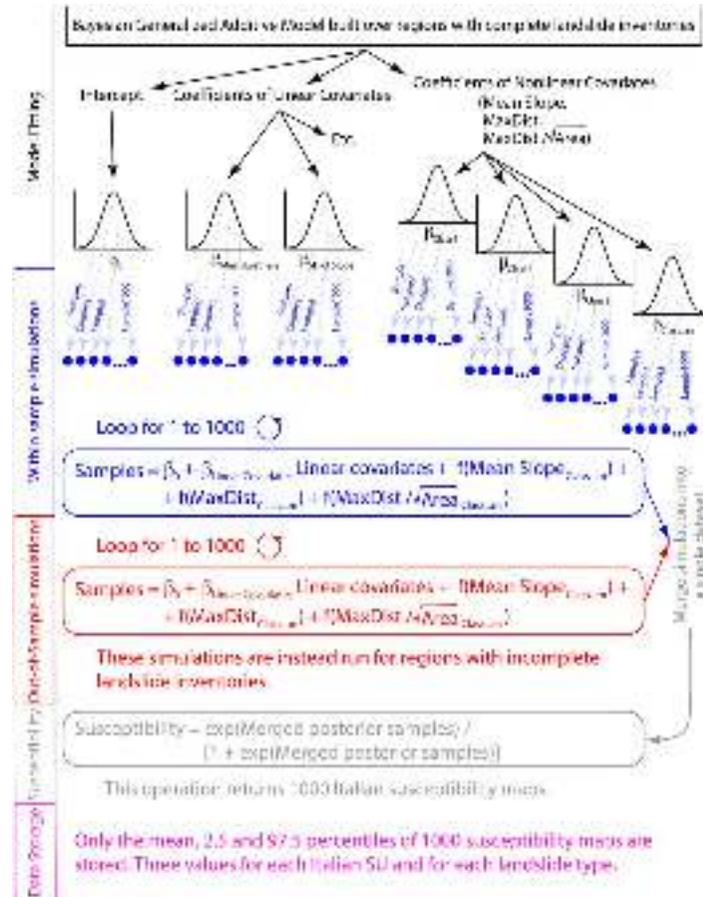
result is very inhomogeneous!

Is it suitable to train a national
susceptibility map?



Loche et al., Earth-Sci. Rev. (2022)

P2. LANDSLIDE SUSCEPTIBILITY: THE CASE OF ITALY



Loche et al., Earth-Sci. Rev. (2022)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



- Spatial aggregation is crucial for presentation of the results

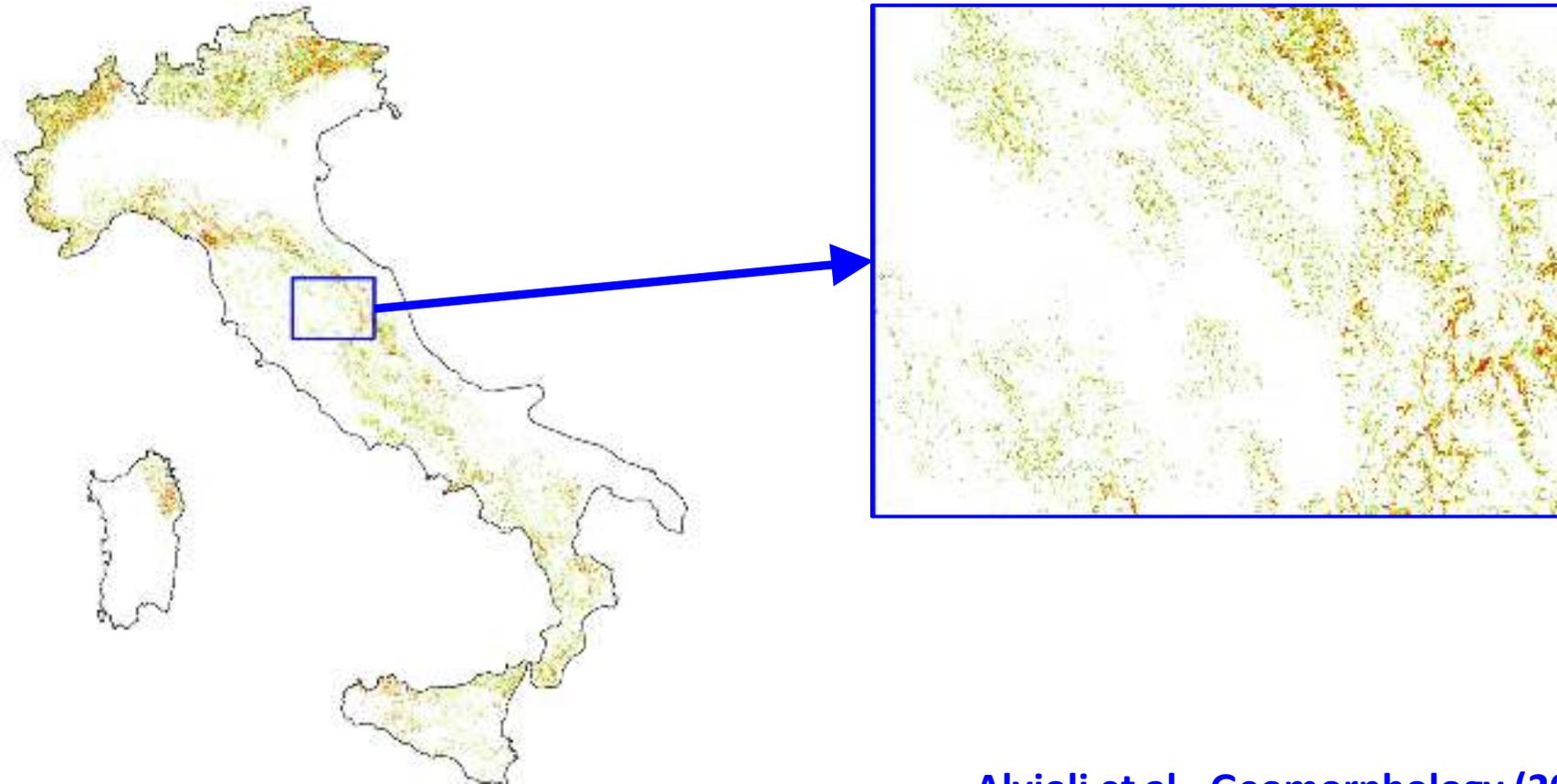
Alvioli et al., *Geomorphology* (2023)

M. Alvioli



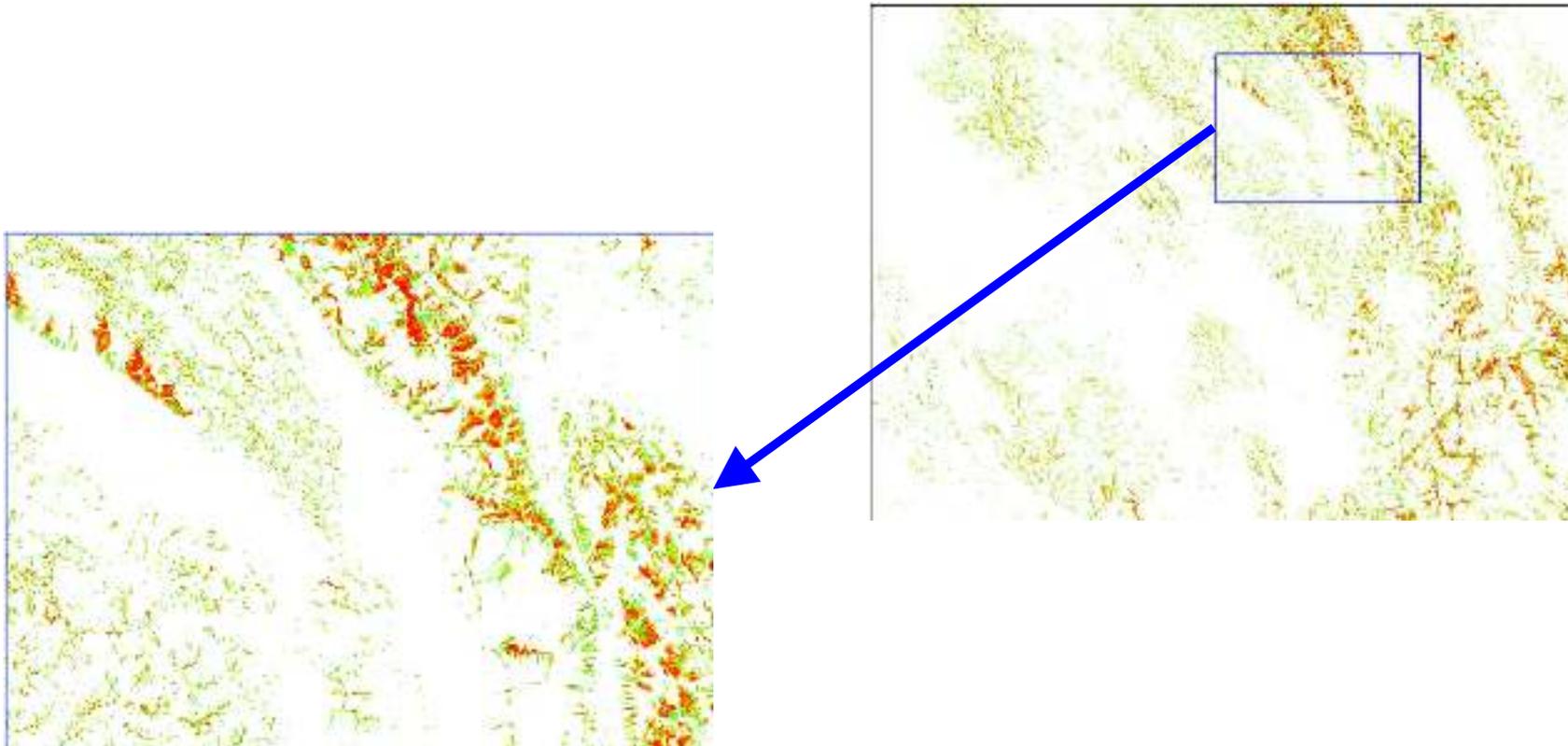
56

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



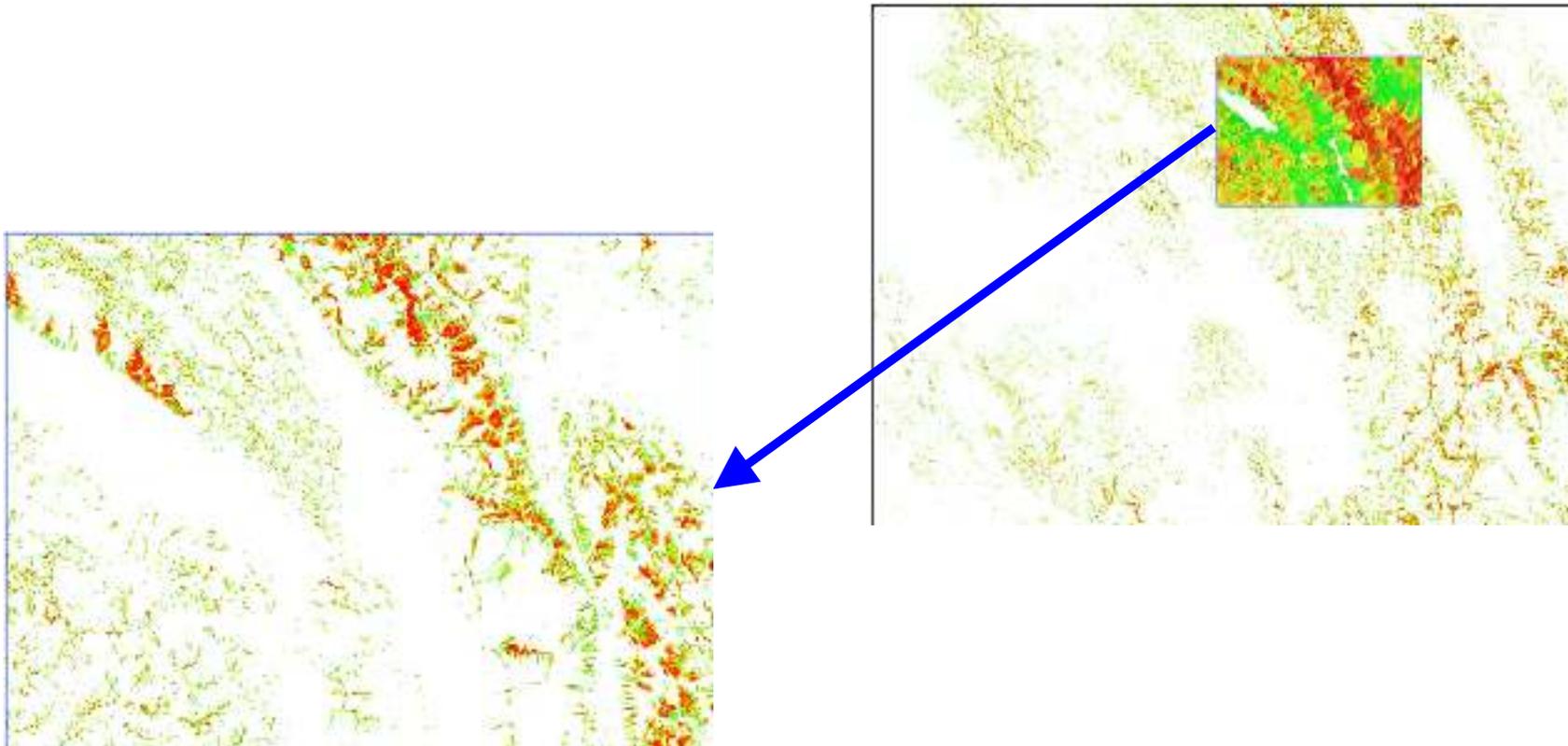
Alvioli et al., *Geomorphology* (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



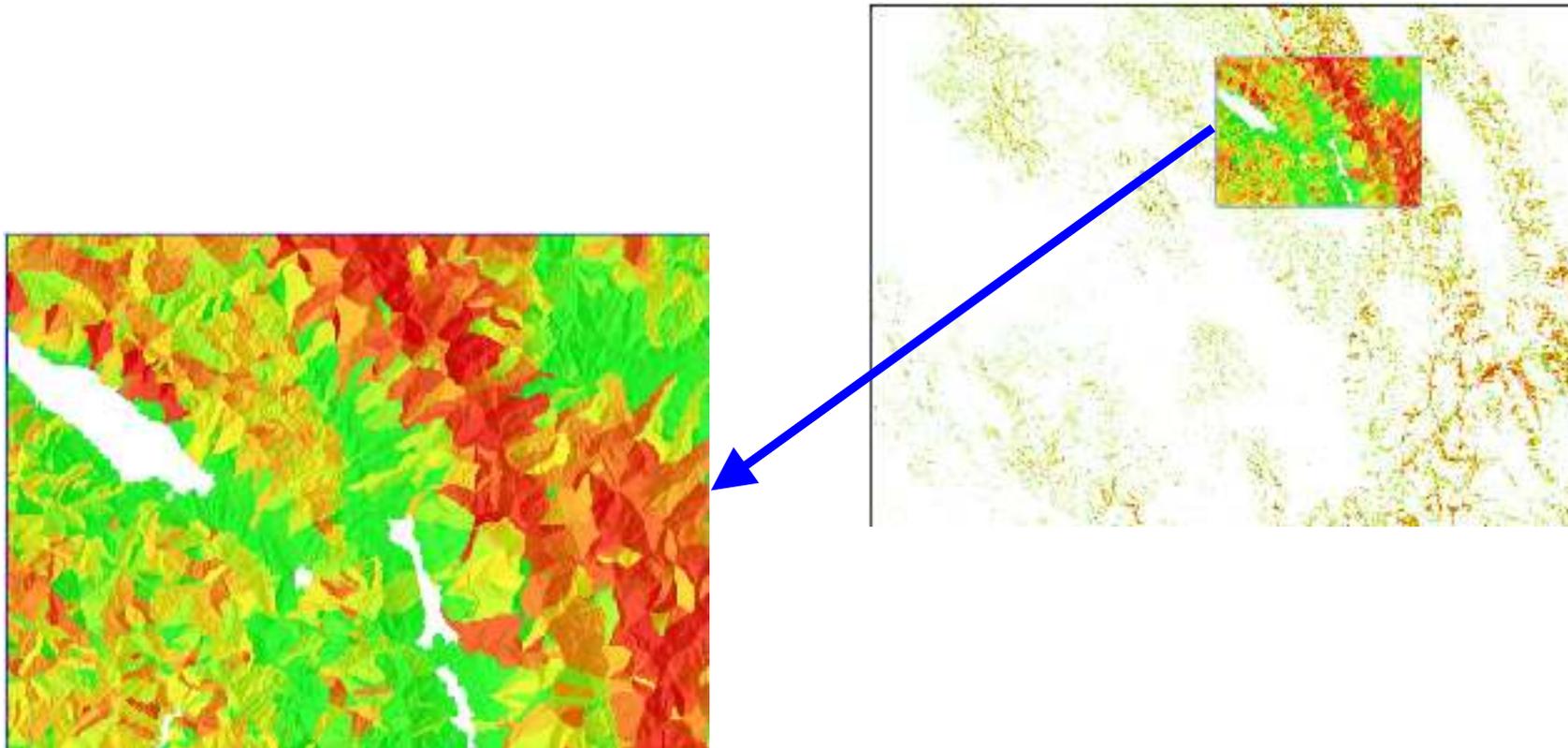
Alvioli et al., *Geomorphology* (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



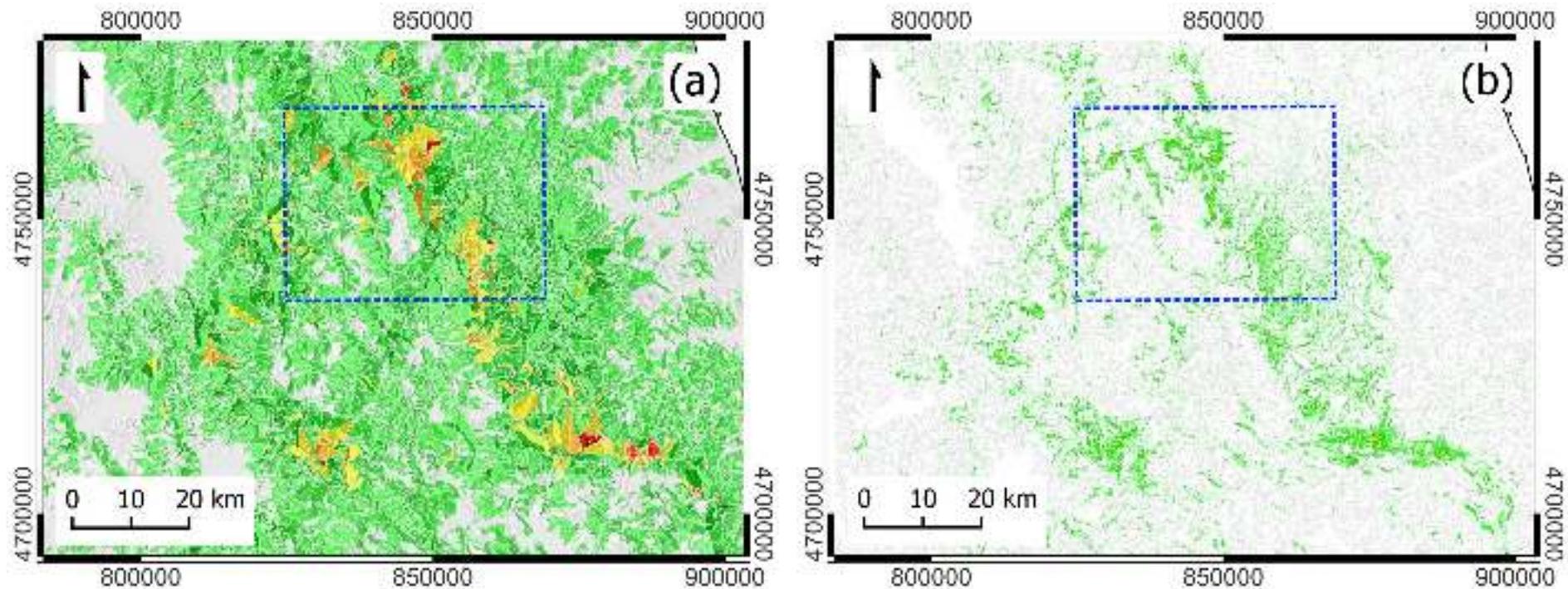
Alvioli et al., *Geomorphology* (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



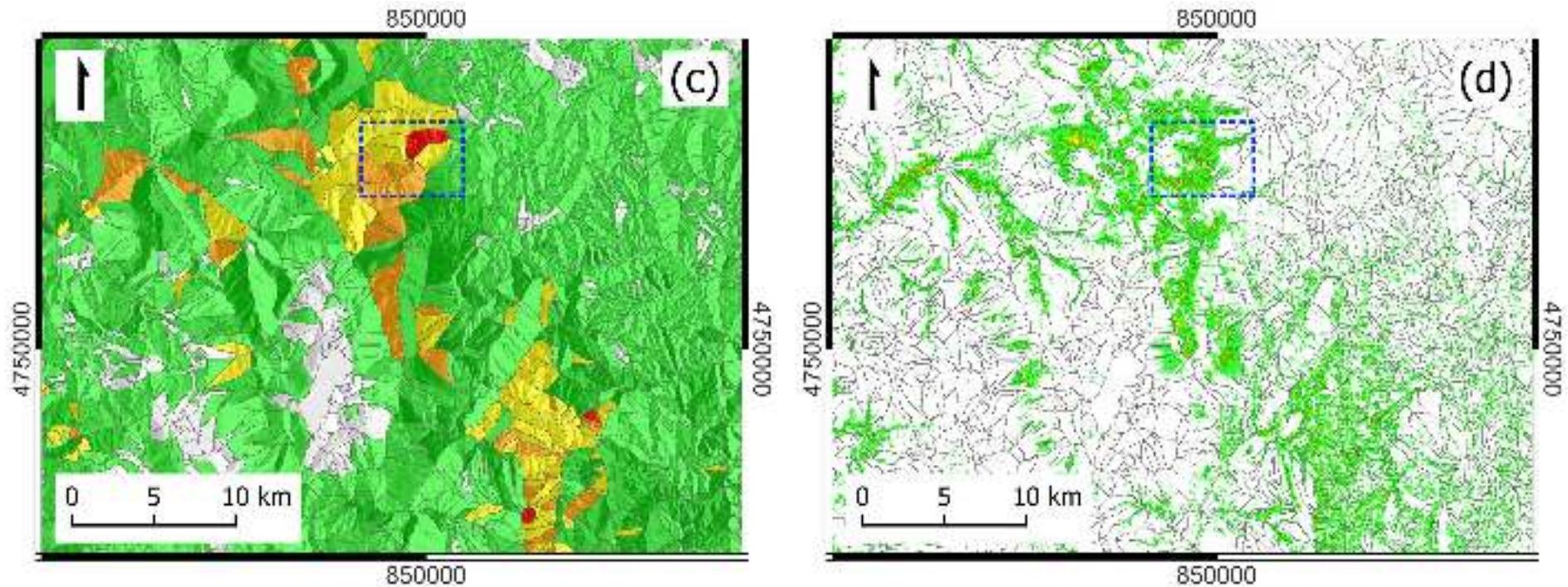
Alvioli et al., *Geomorphology* (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



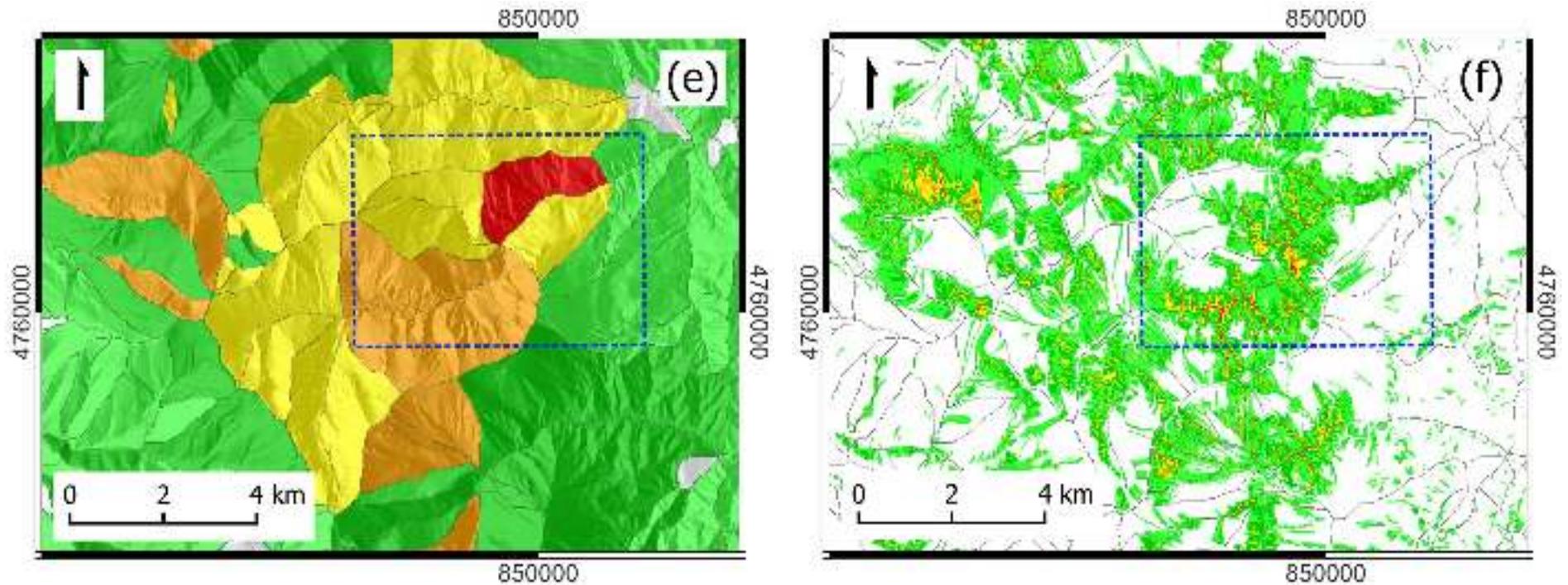
Alvioli et al., Landslides (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



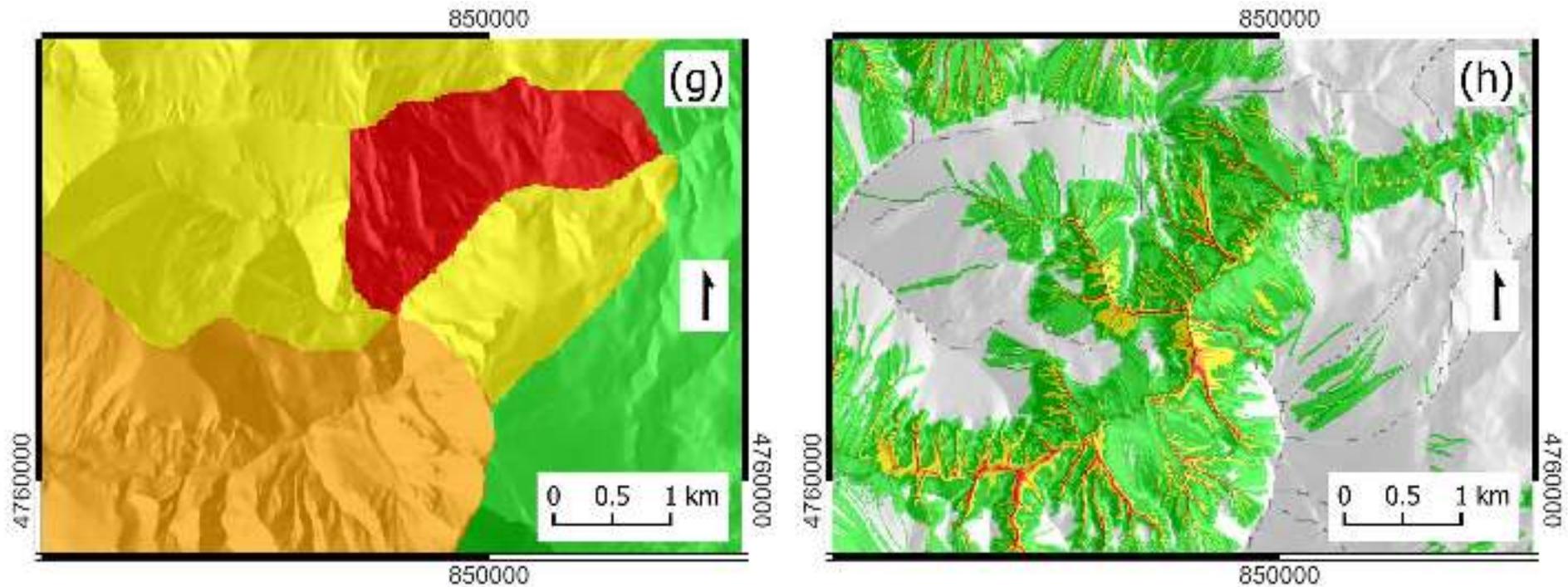
Alvioli et al., Landslides (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



Alvioli et al., Landslides (2023)

P3. NATIONAL ROCKFALL SIMULATION: SPATIAL AGGREGATION



Alvioli et al., Landslides (2023)

P3. APPLICATION TO EARTHQUAKE-INDUCED ROCKFALLS

